

# Can the Fed Control Inflation? Stock Market Implications

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## Abstract

This paper examines the stock market implications of investor uncertainty about the Fed’s inflation-fighting efforts. In a general equilibrium model, investors learn about the Fed’s ability to control inflation. Uncertainty about this ability amplifies volatility and the risk premium, particularly during pronounced monetary tightening and easing cycles. This effect is stronger during tightening, as learning magnifies stock responses to inflation shocks. Moreover, if the Fed’s credibility wanes, investors see inflation as more persistent, boosting volatility and the risk premium. Empirical tests validate the model’s predictions, underscoring the role of learning about the Fed’s inflation management in shaping financial markets.

**Keywords:** Asset Pricing, Learning, Inflation, Federal Reserve, Rate Hikes

**JEL:** D51, D53, G12, G13

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# 1 Introduction

Inflation, a key economic indicator, can disrupt economies and severely impact people’s well-being. The COVID-19 pandemic led to a resurgence of inflation as governments worldwide took drastic measures. Lockdowns, forcing people indoors and businesses to cease operations, impelled governments and central banks to adopt lenient fiscal and monetary policies to support firms and consumers. However, diminished output and a sharp rise in the money supply created an imbalance, sparking inflation. The United States Consumer Price Index (CPI) saw a significant jump one year after lockdowns started, with year-over-year growth hitting 2.6% in March 2021 and exceeding 8.5% in March 2022. In response, the Federal Reserve (henceforth, “the Fed”) began raising interest rates in March 2022.

This raises a crucial question: Can the Fed control inflation? Its capacity to manage inflation profoundly impacts financial markets, investor confidence, and overall economic stability. Absent the Fed’s credibility in combating inflation, the phenomenon risks becoming self-perpetuating. This paper explores the Fed’s credibility issue from investors’ perspective. When investors doubt the Fed’s ability to manage inflation, they gather information from observed inflation data. Integrating this learning process into a general equilibrium model reveals that the market risk premium and volatility increase when the Fed loses its credibility in battling inflation. Furthermore, when the Fed counters high inflation data by hiking interest rates, it precipitates a stock market downturn, increased volatility, and a spike in the market risk premium.

Recent research underscores the significant role of investors’ perceptions of Fed actions in asset pricing. [Bauer, Pflueger, and Sunderam \(2022\)](#) analyze the influence of professional forecasters’ perceptions of the Fed’s monetary policy rule on asset prices and monetary policy transmission, showing that the perceived dependence of the federal funds rate on economic conditions is both time-varying and cyclical. Forecasters adapt their beliefs in response to monetary policy actions. [Caballero and Simsek \(2022\)](#) explore the disagreement between the Fed and financial markets and its impact on interest rate policies and market reactions. [Bianchi, Ludvigson, and Ma \(2022\)](#) explore how Fed announcements influence investor beliefs about evolving monetary policy rules. Together, these works emphasize the importance of understanding how investors assimilate and react to the Fed’s decisions.

Contributing to this line of research, we draw from the literature on learning ([Ai, 2010](#))

and propose a model where a rational agent learns about inflation dynamics, building on [Xiong and Yan \(2010\)](#). We focus on uncertainty and learning about the Fed’s inflation-fighting ability. Our main query is: What are the stock market implications of the agent’s learning about the Fed’s ability to control inflation?

Our analysis employs a general equilibrium economy model ([Lucas, 1978](#)), featuring a representative agent with [Epstein and Zin \(1989\)](#) preferences who consumes the aggregate output. The nominal price of the consumption good acts as a proxy for the consumer price index. In this setting, the Fed adjusts the nominal interest rate based on the Taylor rule, increasing rates in response to inflation growth or signs of overheating. Meanwhile, the agent observes inflation data and updates their beliefs about the Fed’s ability to control inflation via interest rate hikes. As the Fed raises interest rates and a subsequent decline in inflation is observed, the agent’s confidence in the Fed’s ability grows. However, if inflation persists, the agent loses faith in the Fed’s ability, realizing that interest rate hikes are insufficient to curb inflation, ultimately eroding the Fed’s credibility.

The analysis uncovers two novel effects that set our study apart from existing literature. First, we find that uncertainty about the Fed’s ability to control inflation results in higher stock market volatility and risk premium, especially during intense monetary tightening or easing periods. As inflation strays from its target, the Fed’s ability is questioned by the agent, prompting the stock market to react strongly to new information. For instance, a high inflation reading during aggressive tightening may cause a significant market decline, similar to a stock market crash. Conversely, a low inflation reading in the same context could trigger a substantial market rally. This is particularly relevant now, as markets have recently responded strongly to post-COVID inflation data ([Gil de Rubio Cruz, Osambela, Palazzo, Palomino, and Suarez, 2022](#); [Kroner, 2023](#)).

The second effect relates to the agent’s valuation of monetary policy. Assuming a preference for early resolution uncertainty ([Bansal and Yaron, 2004](#)), monetary policy is valuable for the agent because it reduces long-run risk. The Fed tightens during overheating and eases during weakening, stabilizing economic cycles. However, this desirable stabilizing force comes at a cost to the stock market, which negatively correlates with the Fed’s actions: the market falls when the Fed tightens and rises when the Fed eases. In asset-pricing terms, the stock market is considered a “bad” asset due to its negative correlation with a “good” risk, leading the agent to demand a risk premium to hold it. This effect is asymmetric, depending

on whether the cycle is tightening or easing. The agent demands a higher risk premium during tightening because learning amplifies the impact of both positive and negative inflation surprises. For example, a positive inflation surprise during tightening undermines the Fed’s credibility, resulting in doubly bad news. Conversely, during easing, the agent demands a lower risk premium as learning dampens the impact of inflation surprises. As a result, learning leads to a higher risk premium during tightening periods.

The agent’s perception of the Fed’s ability to control inflation strengthens these two effects. This is mainly because the perceived ability directly dictates the degree of long-run risk in the economy. When the perceived ability is low or negative, indicating weaker control by the Fed, it suggests challenges in returning inflation to its long-term mean. Consequently, the agent sees inflation as more persistent, strengthening long-run risk and, in turn, amplifying both the risk premium and stock market volatility.

To quantify these effects, we estimate the parameters of the model using Maximum Likelihood, employing data on U.S. real GDP, Federal funds rate, and inflation rate from 1955 to 2021. Importantly, the estimation does not use any asset prices as inputs. The estimated parameter values yield asset-pricing moments that align with the data. Specifically, the model predicts a real interest rate of 1%, nominal interest rate of 4.5%, market risk premium of 8%, market return volatility of 19%, and market Sharpe ratio of 0.43. We then empirically test the model’s predictions using the S&P 500 as a proxy for the market. Our approach involves multiple steps. Initially, we obtain empirical time series for market risk premium, market return volatility, price-dividend ratio, real interest rate, and expected output growth rate. Subsequently, we derive the model-implied counterparts for these time series by inputting the state variables extracted from the Maximum Likelihood estimation into our theoretical framework.

Using these time series, we find that our model aligns well with the data, showing positive and statistically significant relations between empirical and model-implied quantities. Furthermore, when the Fed tightens, as anticipated by our model, there is a noticeable rise in the empirical real interest rate, expected output growth rate, market risk premium, and market return volatility. Conversely, the empirical market price-dividend ratio declines. These relationships are statistically significant in the data. Moreover, as inflation increases, the empirical real interest rate, expected output growth rate, and market price decrease, mirroring our model’s predictions.

We also find that a decrease in the Fed’s ability to control inflation leads to a statistically significant increase in the empirical market risk premium and market return volatility, in line with the model. Additionally, the data reveals a U-shaped relationship where the risk premium rises during pronounced tightening and easing episodes; however, such a pattern is not evident for volatility. Overall, our empirical findings support the theoretical predictions of the model.

By examining the impact of uncertainty about the Fed’s ability to control inflation, our research adds to the literature on economic policy uncertainty (e.g. [Baker, Bloom, and Davis, 2016](#)). It connects with theories analyzing investor learning and its impact on asset prices ([Timmermann, 1993](#); [Pastor and Veronesi, 2009](#); [Ai, 2010](#)), and in particular with [Pástor and Veronesi \(2013\)](#), who explored the impact of uncertainty regarding future government actions on asset prices. The model we develop stems from the general equilibrium literature ([Lucas, 1978](#)) and explores the interaction between incomplete information ([Detemple, 1986](#)), inflation ([Xiong and Yan, 2010](#); [Cochrane, 2011](#)), interest rates ([Buraschi and Jiltsov, 2005](#); [Wachter, 2006](#)), and asset prices, thereby expanding the literature on asset pricing in monetary economies ([Danthine and Donaldson, 1986](#); [Bakshi and Chen, 1996](#); [Gallmeyer, Hollifield, Palomino, and Zin, 2007](#)).

Our paper builds on previous studies examining the Fed’s role in controlling inflation and maintaining credibility ([Kydland and Prescott, 1977](#); [Alesina and Summers, 1993](#); [Barro and Gordon, 1983](#); [Bernanke and Mishkin, 1997](#); [Bernanke, Laubach, Mishkin, and Posen, 1998](#); [Svensson, 1999](#); [Clarida, Gali, and Gertler, 2000](#); [Woodford, 2003](#); [Walsh, 2017](#)). It also relates to the literature on the effects of monetary policy on financial markets and risk premia ([Gürkaynak, Sack, and Swanson, 2004](#); [Rigobon and Sack, 2004](#); [Bernanke and Kuttner, 2005](#)) and in particular with a growing body of evidence that risk premia respond strongly to the announcement of central banks ([Bianchi et al., 2022](#); [Caballero and Simsek, 2022](#); [Bauer et al., 2022](#); [Bauer and Swanson, 2023](#)).

Our analysis simplifies the complex economic dynamics by focusing on investor learning and the Fed’s ability to control inflation. It omits aspects such as fiscal policy ([Sargent and Wallace, 1981](#); [Leeper, 1991](#)), international trade and exchange rates ([Obstfeld and Rogoff, 1995](#); [Calvo and Reinhart, 2002](#); [Gali and Monacelli, 2005](#)), or the role of a financial intermediation sector in shaping inflation and asset prices ([Bernanke, Gertler, and Gilchrist, 1999](#); [Gertler and Kiyotaki, 2010](#); [Corhay and Tong, 2021](#)). Nevertheless, by emphasizing

the role of investor learning, our research complements the existing literature and encourages further exploration of the interplay between these areas.

The paper proceeds as follows: Section 2 presents our model; Section 3 describes parameter estimation; Section 4 reports results and empirical tests; and Section 5 concludes, summarizing findings and suggesting future research.

## 2 Model

The economy is defined over a continuous-time infinite horizon and consists of a single representative agent who derives utility from consumption. The agent has Kreps-Porteus preferences (Epstein and Zin, 1989; Weil, 1990) with a subjective discount rate  $\rho$ , relative risk aversion  $\gamma$ , and elasticity of intertemporal substitution  $\psi$ . The agent's indirect utility function is given by

$$J_t = \mathbb{E}_t \left[ \int_t^\infty h(C_s, J_s) ds \right],$$

where the aggregator  $h$  is defined as in Duffie and Epstein (1992):

$$h(C, J) = \frac{\rho}{1 - 1/\psi} \left( \frac{C^{1-1/\psi}}{[(1 - \gamma)J]^{1/\theta-1}} - (1 - \gamma)J \right), \quad \text{with } \theta \equiv \frac{1 - \gamma}{1 - 1/\psi}.$$

The aggregate consumption in the economy, denoted by  $\delta$ , follows the dynamic process

$$\frac{d\delta_t}{\delta_t} = \mu_{\delta,t} dt + \sigma_\delta dB_{\delta,t}, \tag{1}$$

where  $\mu_{\delta,t}$  is the expected consumption growth rate,  $\sigma_\delta > 0$  is a known constant, and  $B_\delta$  is a one-dimensional Brownian motion. The expected consumption growth rate  $\mu_{\delta,t}$  varies over time and is determined endogenously from the agent's optimality conditions, as we will show below.

Drawing from the framework introduced by Xiong and Yan (2010)<sup>1</sup>, the consumption

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<sup>1</sup>For other articles that directly model the inflation process, see Wachter (2006), Piazzesi and Schneider (2006), and Bansal and Shaliastovich (2013).

price level,  $p_t$ , evolves according to

$$dp_t/p_t = \pi_t dt,$$

where  $\pi_t$  is the expected rate of inflation, which follows the mean-reverting process:

$$d\pi_t = \lambda_\pi (\bar{\pi}_t - \pi_t) dt + \sigma_\pi dB_{\pi,t}. \quad (2)$$

In equation (2),  $\lambda_\pi > 0$  is a known constant and represents the mean-reversion speed of inflation,  $\sigma_\pi > 0$  is a known constant, and  $B_\pi$  is a one-dimensional Brownian motion uncorrelated with  $B_\delta$ . The long-term inflation expectation,  $\bar{\pi}_t$ , varies over time according to

$$\bar{\pi}_t = \check{\pi} - a_t(r_{N,t} - \bar{r}_N),$$

where  $r_{N,t}$  is the nominal interest rate, whose long-term mean is  $\bar{r}_N$ ,  $\check{\pi}$  is the long-term mean of inflation under neutral interest rates (when  $r_{N,t} = \bar{r}_N$ ), and  $a_t$  is a parameter that governs how inflation responds to deviations of the nominal rate from its long-term mean.

Our model's central assumption is that the Fed governs the long-term inflation expectation  $\bar{\pi}_t$  by setting the nominal interest rate  $r_{N,t}$ . In doing so, the Fed modifies the gap  $\bar{\pi}_t - \pi_t$  in equation (2), which governs the reversion of inflation towards its mean. Importantly, the Fed controls the long-term inflation expectation,  $\bar{\pi}_t$ , and not directly inflation, creating a lag between interest rate changes and the inflation's response to those changes.

Consider an example where, without loss of generality, the expected inflation  $\pi_t$  is high, and the Fed is tightening ( $r_{N,t} - \bar{r}_N > 0$ ). Then, a positive value for the parameter  $a_t$  implies a low  $\bar{\pi}_t$  and a faster reversion of inflation to lower levels. That is, positive values for the parameter  $a_t$  imply that the Fed can control inflation by increasing its mean-reversion speed. Conversely, a negative value for the parameter  $a_t$  weakens the Fed's ability to bring down inflation, meaning that inflation remains sticky and the Fed cannot control it effectively.

The focus of our paper is on the parameter  $a_t$ , which reflects the Fed's *ability* to control inflation. We assume that the representative agent does not observe  $a_t$ . That is, the agent is unsure whether the Fed can bring inflation back down in the near future when it has become

excessively high. The parameter  $a_t$  follows a hidden diffusion process

$$da_t = -\lambda_a a_t dt + \sigma_a dB_{a,t}, \quad (3)$$

where  $\lambda_a > 0$  and  $\sigma_a > 0$  are known constants, and  $B_a$  is a one-dimensional Brownian motion, uncorrelated with  $B_\delta$  and  $B_\pi$ .

The representative agent observes the process of aggregate consumption  $\delta_t$ , nominal interest rates  $r_{N,t}$  set by the Fed, and consumption prices  $p_t$ . Since consumption prices are observable, so is the expected inflation process (2). The history of the expected inflation process together with the history of nominal interest rates allows the agent to learn about Fed's ability to control inflation, i.e., about  $a_t$ . Defining  $\mathcal{F}_t^{\pi, r_N}$  the information set of the agent at time  $t$ , standard filtering theory (Liptser and Shiryaev, 2001) implies that the agent's posterior mean,  $\hat{a}_t \equiv \mathbb{E}[a_t | \mathcal{F}_t^{\pi, r_N}]$ , and the posterior variance,  $\nu_{a,t} \equiv \mathbb{E}[(a_t - \hat{a}_t)^2 | \mathcal{F}_t^{\pi, r_N}]$ , follow

$$d\hat{a}_t = -\lambda_a \hat{a}_t dt - \frac{(r_{N,t} - \bar{r}_N) \lambda_\pi \nu_{a,t}}{\sigma_\pi} d\hat{B}_{\pi,t}, \quad (4)$$

$$d\nu_{a,t} = \left[ \sigma_a^2 - 2\lambda_a \nu_{a,t} - \left( \frac{(r_{N,t} - \bar{r}_N) \lambda_\pi \nu_{a,t}}{\sigma_\pi} \right)^2 \right] dt, \quad (5)$$

where  $\hat{B}_\pi$  is a Brownian motion under agent's filtration and represents a surprise change in expected inflation. Post-filtering, the agent perceives the expected inflation process as

$$d\pi_t = \lambda_\pi \underbrace{[\check{\pi} - \hat{a}_t(r_{N,t} - \bar{r}_N) - \pi_t]}_{\equiv \hat{\pi}_t} dt + \sigma_\pi d\hat{B}_{\pi,t}, \quad (6)$$

where  $\hat{\pi}_t \equiv \check{\pi} - \hat{a}_t(r_{N,t} - \bar{r}_N)$  is the agent's long-term inflation expectation. Of course, the agent's long-term inflation expectation depends on the agent's estimate of the Fed's ability to control inflation.

The agent's updating of beliefs in Equation (4) depends on the difference  $r_{N,t} - \bar{r}_N$ . To fix ideas, assume that the Fed is tightening, meaning that  $r_{N,t} > \bar{r}_N$ . Then a positive surprise change in expected inflation ( $d\hat{B}_{\pi,t} > 0$ , or an inflationary shock) lowers the agent's estimate  $\hat{a}_t$ . The agent's confidence in Fed's ability to control inflation decreases after the inflationary shock because inflation keeps rising despite the Fed's tightening. If, on the contrary, the



agent observes a negative surprise change in expected inflation—a deflationary shock—then  $\hat{a}_t$  increases, restoring the agent’s confidence in Fed’s ability to fight inflation.

We observe an asymmetric response of  $\hat{a}_t$  to inflation surprises. When the Fed is tightening, a positive inflation surprise not only represents bad news but also lowers the agent’s estimate  $\hat{a}_t$  or their perception of the Fed’s ability to control inflation. Conversely, in the case of an easing episode, the same positive surprise in inflation leads the agent to perceive an improvement in the Fed’s ability to bring inflation back to its long-term mean. This asymmetric response of  $\hat{a}_t$  will be relevant for some of our asset pricing results.

The posterior uncertainty  $\nu_{a,t}$  evolves locally deterministically over time as described in (5). It tends to increase when interest rates are close to being neutral ( $r_{N,t} \approx \bar{r}_N$ ) because valuable information about the Fed’s ability to control inflation can only be observed when the Fed tries to either fight inflation ( $r_{N,t} > \bar{r}_N$ ) or increase inflation ( $r_{N,t} < \bar{r}_N$ ). Importantly, the posterior uncertainty never vanishes since the agent learns about a moving target, which evolves as in (3). As shown below,  $\nu_{a,t}$  is the channel through which the agent’s confidence in the Fed’s ability to control inflation generates novel asset pricing results.

The Fisher equation states that the nominal interest rate  $r_{N,t}$  must equal the sum of the real interest rate  $r_{R,t}$  and the expected inflation rate:

$$r_{N,t} = r_{R,t} + \pi_t. \quad (7)$$

In this economy, the Fed relies on the Taylor rule to guide its response to deviations in inflation and economic growth (Taylor, 1993, 1999). The agent is aware of and observes the Taylor rule. However, the agent recognizes that economies are not static; they evolve, and as they change, the tools and strategies once effective might not remain so. Thus, our central hypothesis is that despite observing the Taylor rule, the agent questions its current efficacy in managing inflation, as previously discussed.<sup>2</sup>

The Taylor rule relies on two positive and known constants, namely  $\beta_\pi$  and  $\beta_\mu$ . Specifically, if the recent history of inflation and economic growth deviate from their target levels,

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<sup>2</sup>A related question is to assume that the Taylor rule’s coefficients are unknown and examine how the agent interprets them. This perspective would highlight the agent’s perception of the Fed’s responsiveness to inflation or growth. However, our study’s scope is broader. Rather than delving into the individual components of the Taylor rule, we focus on a more overarching question: Can the Fed effectively control inflation when employing a standard Taylor rule?

the Fed changes the nominal interest rate according to:

$$r_{N,t} = \bar{r}_N + \beta_\pi (\phi_{\pi,t} - \bar{\pi}) + \beta_\mu (\phi_{\mu,t} - \bar{\mu}_\delta). \quad (8)$$

The Taylor rule considers the difference between the current *inflation index*  $\phi_{\pi,t}$  and the targeted inflation rate  $\bar{\pi}$ , and the difference between the current *consumption growth index*  $\phi_{\mu,t}$  and the natural expected consumption growth rate  $\bar{\mu}_\delta = \frac{\mathbb{E}(d\delta_t/\delta_t)}{dt}$ . The inflation index,  $\phi_{\pi,t}$ , is based on the history of observations of the price level, while the consumption growth index,  $\phi_{\mu,t}$ , is based on the history of observations of the aggregate consumption:

$$\phi_{\pi,t} = \omega_\pi \int_0^t e^{-\omega_\pi(t-s)} \frac{dp_s}{p_s}, \quad (9)$$

$$\phi_{\mu,t} = \omega_\mu \int_0^t e^{-\omega_\mu(t-s)} \frac{d\delta_s}{\delta_s}. \quad (10)$$

In the real world, unlike in this continuous-time setup, the Fed doesn't have access to instantaneous expected inflation or instantaneous expected growth. Instead, it typically relies on aggregate data, which may be collected and reported over a month or a quarter. The indices  $\phi_{\pi,t}$  and  $\phi_{\mu,t}$  can be seen as mathematical tools to represent this aggregation. The indices essentially accumulate the historical data, giving more weight to recent information. To further understand their meaning, note first that (9) and (10) imply the following dynamics:

$$d\phi_{\pi,t} = \omega_\pi (\pi_t - \phi_{\pi,t}) dt, \quad (11)$$

$$d\phi_{\mu,t} = \omega_\mu (\mu_{\delta,t} - \phi_{\mu,t}) dt + \omega_\mu \sigma_\delta dB_{\delta,t}, \quad (12)$$

where it can be shown that the unconditional means of  $\phi_{\pi,t}$  and  $\phi_{\mu,t}$  are respectively  $\bar{\pi}$  and  $\bar{\mu}_\delta$ . Consider now a discretization of (11) with time steps  $\Delta t$ :

$$\phi_{\pi,t} = (1 - e^{-\omega_\pi \Delta t}) \sum_{n=0}^{\infty} e^{-\omega_\pi n \Delta t} \pi_{t-n\Delta t}. \quad (13)$$

The expression (13) resembles an exponential moving average, with the parameter  $\omega_\pi$  driving the weight associated with the present relative to the past. If  $\omega_\pi$  is large, the past price growth

influences to a small degree the index, causing it to closely represent current price growth. On the other hand, if  $\omega_\pi$  is small, the past history of price growth influences the index to a greater extent. This logic also applies to the index  $\phi_{\mu,t}$ , with the added impact of  $B_\delta$  shocks, reminiscent of an ARMA model. In fact, discretizing (12) produces:

$$\phi_{\mu,t} = (1 - e^{-\omega_\mu \Delta t}) \sum_{n=0}^{\infty} e^{-\omega_\mu n \Delta t} \mu_{\delta,t-n\Delta t} + \omega_\mu \sigma_\delta \sqrt{\frac{1 - e^{-\omega_\mu \Delta t}}{2\omega_\mu}} \sum_{n=0}^{\infty} e^{-\omega_\mu n \Delta t} Z_{t-n\Delta t},$$

where  $Z$  is the  $N(0, 1)$  discrete counterpart of the Brownian  $B_\delta$ . The parameter  $\omega_\mu$  controls the weight associated with the present consumption growth relative to the past, with a higher  $\omega_\mu$  giving more weight to recent data.

To summarize, the indices  $\phi_{\pi,t}$  and  $\phi_{\mu,t}$  allow the Fed to base its interest rate decision not only on the latest estimates of inflation and expected consumption growth but on their entire history. The Taylor rule is thus versatile, permitting the Fed to adjust the weight it assigns to past observations. The parameter values  $\omega_\pi$ ,  $\omega_\mu$ ,  $\beta_\pi$ , and  $\beta_\mu$  will be estimated from the data in Section 3.

A convenient simplification arises when  $\omega_\pi = \omega_\mu \equiv \omega$ . The dynamics of the variable

$$\phi_t \equiv \beta_\pi (\phi_{\pi,t} - \bar{\pi}) + \beta_\mu (\phi_{\mu,t} - \bar{\mu}_\delta),$$

which enters the Taylor rule in (8), do not include the two indices  $\phi_{\pi,t}$  and  $\phi_{\mu,t}$ :

$$d\phi_t = \omega[\beta_\mu(\mu_{\delta,t} - \bar{\mu}_\delta) + \beta_\pi(\pi_t - \bar{\pi}) - \phi_t]dt + \omega\beta_\mu\sigma_\delta dB_{\delta,t}. \quad (14)$$

The dynamics in (14) show that  $\phi_t$  mean-reverts at speed  $\omega$  towards its stochastic mean, which is determined by the weighted sum of the inflation and consumption growth deviations from their targets. This reduction of  $\phi_{\pi,t}$  and  $\phi_{\mu,t}$  into a single state variable  $\phi_t$  when  $\omega_\pi = \omega_\mu \equiv \omega$  simplifies the numerical method and facilitates our interpretations. In essence, high values of  $\phi_t$  indicate tightening, and low values indicate easing. Since eliminating one state variable simplifies the numerical solution of the equilibrium and helps us to interpret our findings more easily, we assume going forward that  $\omega_\pi = \omega_\mu \equiv \omega$ .<sup>3</sup> Hereafter,  $\phi_t$  will be

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<sup>3</sup>Evidence confirming that the estimated values of the mean-reversion speeds  $\omega_\pi$  and  $\omega_\mu$  are almost identical will be provided in Section 3.

referred to as the *Fed tightening index*.

This implies that the nominal interest rate is determined by:

$$r_{N,t} = \bar{r}_N + \phi_t, \quad (15)$$

with the dynamics of  $\phi_t$  provided in (14).

We observe that the process  $\phi_t = r_{N,t} - \bar{r}_N$  has a direct impact on the agent's updating of beliefs in equation (4). This establishes a clear connection between the Fed's decisions, as governed by (15), and the agent's learning process regarding the Fed's ability to control inflation, as described in (4).

Solving for the equilibrium in this economy involves writing the HJB equation:

$$\max_C \{h(C, J) + \mathcal{L}J\} = 0, \quad (16)$$

with the differential operator  $\mathcal{L}J$  following from Itô's lemma. In keeping with existing work (e.g., [Benzoni, Collin-Dufresne, and Goldstein, 2011](#)), we guess the following value function:

$$J(C, \pi, \hat{a}, \phi, \nu_a) = \frac{C^{1-\gamma}}{1-\gamma} [\rho e^{I(x_t)}]^\theta, \quad (17)$$

where  $I(x_t)$  is the log wealth-consumption ratio and  $x_t \equiv [\pi_t \ \hat{a}_t \ \phi_t \ \nu_{a,t}]^\top$  denotes the state vector. (Note that the state vector does not include  $\mu_{\delta,t}$ , which in our model will be endogenously determined in equilibrium as a function of the other state variables.)

Substituting the guess (17) into the HJB Equation (16) and imposing the market-clearing condition  $C_t = \delta_t$ , yields a partial differential equation for the log wealth-consumption ratio. We numerically solve this equation using Chebyshev polynomials ([Judd, 1998](#)). Appendix A describes the solution method and details the numerical procedure.

**Equilibrium market price of risk and real risk-free rate** Following [Duffie and Epstein \(1992\)](#), the state price density in this economy is given by

$$\xi_t = \exp \left[ \int_0^t h_J(C_s, J_s) ds \right] h_C(C_t, J_t) = \exp \left[ \int_0^t \left( \frac{\theta - 1}{e^{I(x_s)}} - \rho \theta \right) ds \right] \rho^\theta C_t^{-\gamma} (e^{I(x_t)})^{\theta-1}.$$

A two-dimensional Brownian vector,  $\hat{B}_t \equiv [B_{\delta,t} \ \hat{B}_{\pi,t}]^\top$ , drives the state variables in this

economy. As a result, the market price of risk in this economy is also two-dimensional, denoted as  $m_t \equiv [m_{\delta,t} \ m_{\pi,t}]^\top$ . Both the market price of risk and the real risk-free rate  $r_{R,t}$  result from the dynamics of the state price density,

$$\frac{d\xi_t}{\xi_t} = -r_{R,t}dt - m_t^\top d\widehat{B}_t, \quad (18)$$

Itô's Lemma yields the market prices of risk for  $B_\delta$  and  $\widehat{B}_\pi$ :

$$m_{\delta,t} = \gamma\sigma_\delta + (1 - \theta)\sigma_\delta\beta_\mu\omega I_\phi, \quad (19)$$

$$m_{\pi,t} = (1 - \theta) \left( \sigma_\pi I_\pi - \frac{\lambda_\pi \nu_{a,t}}{\sigma_\pi} I_{\widehat{a}} \phi_t \right), \quad (20)$$

where we denote by  $I_z$  the partial derivative of the log wealth-consumption ratio with respect to the state variable  $z \in \{\pi, \widehat{a}, \phi, \nu_a\}$ .

Focusing on the market price of risk  $m_{\delta,t}$ , the Fed's monetary policy plays an important role in mitigating growth fluctuations caused by  $B_\delta$ . The Fed tightens when facing an overheating economy (high  $\phi_t$ ), leading to an expected negative sign for  $I_\phi$ . Conversely, the Fed eases when facing a weak economy, also implying  $I_\phi < 0$ . (We will confirm the assumed signs of the partial derivatives of  $I(x_t)$  in Section 4.) The agent values the Fed's stabilizing force through the long-run risk channel, with  $1 - \theta$  measuring the preference for early resolution of uncertainty. From the long-run risk agent's perspective, the Fed's response to changes in  $\phi_t$  reduces long-run risk and, with it,  $m_{\delta,t}$ . This effect is stronger as  $\sigma_\delta$  (the scale of economic fluctuations),  $\beta_\mu$  (the output gap coefficient in the Taylor rule), and  $\omega$  (the weight given to recent growth data) increase.

For the market price of risk  $m_{\pi,t}$ , we expect a negative  $I_\pi$  (as higher inflation reduces expected real consumption growth and the wealth-consumption ratio) and a positive  $I_{\widehat{a}}$  (since greater trust in the Fed's inflation control ability raises the wealth-consumption ratio). Assuming the Fed is tightening ( $\phi_t > 0$ ) and considering the signs  $I_\pi < 0$  and  $I_{\widehat{a}} > 0$ , we obtain a negative  $m_{\pi,t}$ . Consequently, the agent is willing to pay a premium for assets whose returns covary positively with inflation. The magnitude of the price of risk  $m_{\pi,t}$  grows with a strong preference for early resolution of uncertainty (large  $1 - \theta$ ), with higher inflation volatility (large  $\sigma_\pi$ ), and, crucially, with higher uncertainty in the Fed's inflation control ability (large  $\nu_{a,t}$ ).

Itô's Lemma applied to (18) yields the equilibrium real risk-free rate:

$$r_{R,t} = \rho + \frac{\mu_{\delta,t}}{\psi} - \frac{\gamma(1+\psi)}{2\psi}\sigma_{\delta}^2 - \frac{1-\theta}{2}(\sigma_{W,t}^2 - \sigma_{\delta}^2), \quad (21)$$

where  $\sigma_{W,t}^2$  is the instantaneous variance of wealth,

$$\sigma_{W,t}^2 \equiv \sigma_{\delta}^2 + 2\sigma_{\delta}^2\beta_{\mu}\omega I_{\phi} + \sigma_{\pi}^2 I_{\pi}^2 + \frac{\lambda_{\pi}^2 \nu_{a,t}^2 \phi_t^2}{\sigma_{\pi}^2} I_{\hat{a}}^2 + \sigma_{\delta}^2 \beta_{\mu}^2 \omega^2 I_{\phi}^2 - 2\lambda_{\pi} \nu_{a,t} \phi_t I_{\pi} I_{\hat{a}}.$$

The first two terms in (21) are familiar drivers of the real risk-free rate: the time preference rate and the expected growth rate of consumption. The last two terms result from precautionary saving and represent an adjustment for risk, which includes consumption risk and excess wealth risk. The last term vanishes in the CRRA case ( $\theta = 1$ ).

Replacing  $r_{R,t}$  in the Fisher equation (7), then fixing  $r_{N,t} = \bar{r}_N$  and taking unconditional expectations on both sides determines the neutral level of interest rates,  $\bar{r}_N$ , as a known function of the other parameters:

$$\bar{r}_N = \rho + \bar{\pi} + \frac{\bar{\mu}_{\delta}}{\psi} - \frac{\gamma(1+\psi)}{2\psi}\sigma_{\delta}^2 - \frac{1-\theta}{2} \left( 2\sigma_{\delta}^2\beta_{\mu}\omega \bar{I}_{\phi} + \sigma_{\pi}^2 \bar{I}_{\pi}^2 + \sigma_{\delta}^2 \beta_{\mu}^2 \omega^2 \bar{I}_{\phi}^2 \right),$$

where  $\bar{I}_{\pi}$  and  $\bar{I}_{\phi}$  are the values of the partial derivatives of the log wealth-consumption ratio measured when all state variables are at their long-term means:  $\pi = \bar{\pi}$ ,  $\hat{a} = 0$ ,  $\phi = 0$ , and  $\nu_a = \bar{\nu}_a$ .

In our economy, the expected growth rate of consumption is endogenously determined in equilibrium and depends on monetary policy. Equation (21), together with the Fisher equation (7), lead to an equilibrium expected growth rate:

$$\mu_{\delta,t} = \underbrace{\psi(r_{N,t} - \pi_t - \rho)}_{r_{R,t}} + \frac{\gamma(1+\psi)}{2}\sigma_{\delta}^2 + \frac{\psi(1-\theta)}{2}(\sigma_{W,t}^2 - \sigma_{\delta}^2). \quad (22)$$

Equation (22) determines the expected growth as a function of the nominal rate and expected inflation. Meanwhile, equation (6) describes the inflation path based on the agent's perceived impact of the Fed's decisions. In order to close the model, these two equations are supplemented with the Taylor rule (15), which determines the nominal interest rate

$r_{N,t}$ . Collectively, these three equations imply that the real consumption's equilibrium path depends on monetary policy, making the expected consumption growth  $\mu_{\delta,t}$  endogenous and monetary policy non-neutral.

Given this, in our model with learning about the Fed's ability to control inflation, monetary policy becomes non-neutral in equilibrium. This approach, which starts with a semi-exogenous inflation process and solves for the equilibrium expected growth, introduces non-neutrality without resorting to standard mechanisms commonly found in traditional New Keynesian models, such as those described in Galí (2015).

In equation (22), the nominal interest rate does not move one-for-one with expected inflation<sup>4</sup>, resulting in fluctuations in  $r_{R,t}$ . These changes in the real interest rate, in turn, impact consumption since the representative agent adjusts her expected future consumption growth to align with the new real interest rate level. To illustrate this, let us consider the log level of real consumption, denoted by  $c_t = \log(\delta_t)$ . By discretizing equation (1) and using equation (22), we can write  $\mathbb{E}_t[c_{t+1}] - c_t = \mu_{\delta,t} - \sigma_{\delta}^2/2$ , which implies:

$$c_t - \mathbb{E}_t[c_{t+1}] = \psi(\rho + \pi_t - r_{N,t}) - \left( \frac{\gamma(1 + \psi)}{2\psi} + \frac{1}{2} \right) \sigma_{\delta}^2 - \frac{\psi(1 - \theta)}{2} (\sigma_{W,t}^2 - \sigma_{\delta}^2). \quad (23)$$

The optimality condition (23), arising from the representative agent's first-order condition for consumption today versus consumption tomorrow, aligns with conditions found in standard monetary policy frameworks (e.g., Galí, 2015, Chapter 3, p. 54). According to this condition, the agent consumes more today relative to tomorrow when either the subjective discount rate  $\rho$  or the inflation rate  $\pi_t$  is high, and consumes less today relative to tomorrow when the nominal interest rate  $r_{N,t}$  is high.

The final term in Equation (23) acts as the “exogenous preference shifter” in monetary economies. A change in this term can be interpreted as a discount rate shock (Galí, 2015, Chapter 3). A key difference in our model is that this shock is endogenous and driven by the excess variance of wealth,  $\sigma_{W,t}^2 - \sigma_{\delta}^2$ . An increase in the excess variance of wealth results in lower consumption today relative to tomorrow because the representative agent prefers early resolution of uncertainty. As such, a higher excess variance of wealth boosts precautionary

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<sup>4</sup>Applying Itô's Lemma to the Taylor rule equation (8) shows that the nominal interest rate depends on the Brownian  $B_{\delta}$ , while expected inflation  $\pi_t$  solely depends on the Brownian  $B_{\pi}$  as given in equation (2). Therefore, based on the Fisher equation (7), a change in expected inflation must result in a change in the real interest rate. In other words, monetary policy is non-neutral.

saving and discourages current consumption.

**Equilibrium asset prices** As in [Bansal and Yaron \(2004\)](#), we will now consider an asset (the “market”) that pays an aggregate dividend, which follows the dynamic process

$$\frac{dD_t}{D_t} = [(1 - \alpha)\bar{\mu}_\delta + \alpha\mu_{\delta,t}]dt + \sigma_D dB_{D,t}, \quad (24)$$

where  $B_D$  is a one-dimensional Brownian motion uncorrelated with  $\{B_\delta, \hat{B}_\pi\}$ ,  $\alpha$  is the dividend leverage on expected consumption growth ([Abel, 1999](#)), and  $\sigma_D$  helps calibrate the volatility of dividends which in the data is larger than that of consumption. Assuming non-zero correlations between  $B_D$  and  $\{B_\delta, \hat{B}_\pi\}$  is possible but not necessary to achieve our main objective of isolating the impact of learning about the Fed on asset prices. In equation (24), the expected growth rate of dividends is an affine function of the economy’s expected growth rate,  $\mu_{\delta,t}$ . As inflation and monetary policy impact  $\mu_{\delta,t}$ , we will analyze how asset pricing reflects this impact. Lastly, the constant  $(1 - \alpha)\bar{\mu}_\delta$  in the drift of (24) ensures that the average dividend growth rate is equal to the average consumption growth rate,  $\bar{\mu}_\delta$ .

Denote the log price-dividend ratio by  $\Pi(x_t)$ , which solves a partial differential equation we relegate to [Appendix A](#). The diffusion of market returns is a vector with three elements:

$$s_{\delta,t} = \sigma_\delta \beta_\mu \omega \Pi_\phi, \quad (25)$$

$$s_{\pi,t} = \sigma_\pi \Pi_\pi - \frac{\lambda_\pi \nu_{a,t}}{\sigma_\pi} \Pi_{\hat{a}} \phi_t, \quad (26)$$

$$s_{D,t} = \sigma_D.$$

Multiplying each of the market prices of risk in (19)-(20) with the corresponding diffusions in (25)-(26), then taking the sum, yields the market risk premium (the market price of risk for  $B_D$  is zero, and thus  $\sigma_D$  does not enter the risk premium):

$$\begin{aligned} RP_t = & \gamma \sigma_\delta^2 \beta_\mu \omega \Pi_\phi + (1 - \theta) \sigma_\delta^2 \beta_\mu^2 \omega^2 \Pi_\phi I_\phi + (1 - \theta) \sigma_\pi^2 \Pi_\pi I_\pi \\ & - (1 - \theta) \nu_{a,t} (\Pi_\pi I_{\hat{a}} + \Pi_{\hat{a}} I_\pi) \lambda_\pi \phi_t + (1 - \theta) \frac{\lambda_\pi^2 \nu_{a,t}^2}{\sigma_\pi^2} \Pi_{\hat{a}} I_{\hat{a}} \phi_t^2. \end{aligned} \quad (27)$$

In line with our analysis of the log wealth-consumption ratio, we hypothesize—and con-



firm in Section 4—that:  $\Pi_\phi < 0$  (the Fed tightens during an overheating economy and eases during a weakening economy, resulting in a negative relationship between  $\phi_t$  and asset prices);  $\Pi_{\hat{a}} > 0$  (confidence in the Fed’s ability to control inflation boosts asset prices); and  $\Pi_\pi < 0$  (inflation reduces growth and negatively affects asset prices).

Two primary factors influence the risk premium. First, for the long-run risk agent, the Fed’s monetary policy lowers the market price of  $B_\delta$  risk—refer to our discussion of equation (19)—resulting in  $I_\phi < 0$ . Consequently, the term  $(1 - \theta)\sigma_\delta^2\beta_\mu^2\omega^2\Pi_\phi I_\phi$  in (27) is positive. In other words, the Fed’s tightening or easing policy reduces long-run risk and is thus favorable. However, the market declines when the Fed tightens (when  $\phi$  increases) and rises when the Fed eases (when  $\phi$  decreases), creating a negative correlation between  $B_\delta$  and the market, which leads to a positive risk premium. The magnitude of this effect on the risk premium depends on the agent’s perceived confidence in the Fed’s ability to control inflation,  $\hat{a}_t$ . To gain some intuition why, suppose  $\hat{a}_t$  is positive and large. In that case, the Fed’s strong ability to control inflation will promptly bring it back to its long-term mean, making it less persistent. This weakens the impact of long-run risk and thus the risk premium. Further discussion on this effect can be found in Section 4.

The uncertainty channel  $\nu_{a,t}$  is the second factor affecting the market risk premium. It is represented by the second-row terms in equation (27), which form a quadratic expression in the Fed tightening index  $\phi_t$ . The product  $\Pi_{\hat{a}}I_{\hat{a}}$  is positive, and thus the quadratic term generates a U-shape. This means that uncertainty about the Fed’s ability to control inflation increases the risk premium when the Fed deviates from a neutral monetary policy. Moreover, the linear term in  $\phi_t$  leads to an asymmetric response. Since  $\Pi_\pi I_{\hat{a}} + \Pi_{\hat{a}}I_\pi < 0$ , the risk premium is higher during a tightening cycle than during an easing cycle. This asymmetry follows from equation (4), which shows that learning amplifies the impact of inflation surprises during tightening episodes and dampens it during easing episodes.

Finally, the risk premium is magnified by the term  $(1 - \theta)\sigma_\pi^2\Pi_\pi I_\pi$ , which is positive when both the aggregate wealth and the market decrease with inflation, in other words, when  $\Pi_\pi < 0$  and  $I_\pi < 0$ . All the above effects are more pronounced when there is high uncertainty, the economy is in a more extreme tightening or easing cycle, or the agent strongly prefers early resolution of uncertainty.

These two forces driving the risk premium reflect our paper’s main contributions. The first force is based on the idea that the Fed’s monetary policy stabilizes aggregate fluctuations

and is therefore desirable in a long-run risk economy. However, the market bears a cost in the form of a risk premium, especially when the Fed’s ability to control inflation,  $\hat{a}_t$ , is low or negative. The second force is based on the idea that the agent is uncertain about the Fed’s ability to control inflation. This uncertainty increases the risk premium when the Fed deviates from a neutral monetary policy, creating concerns that the Fed may not be able to bring inflation back to target, particularly during tightening periods.

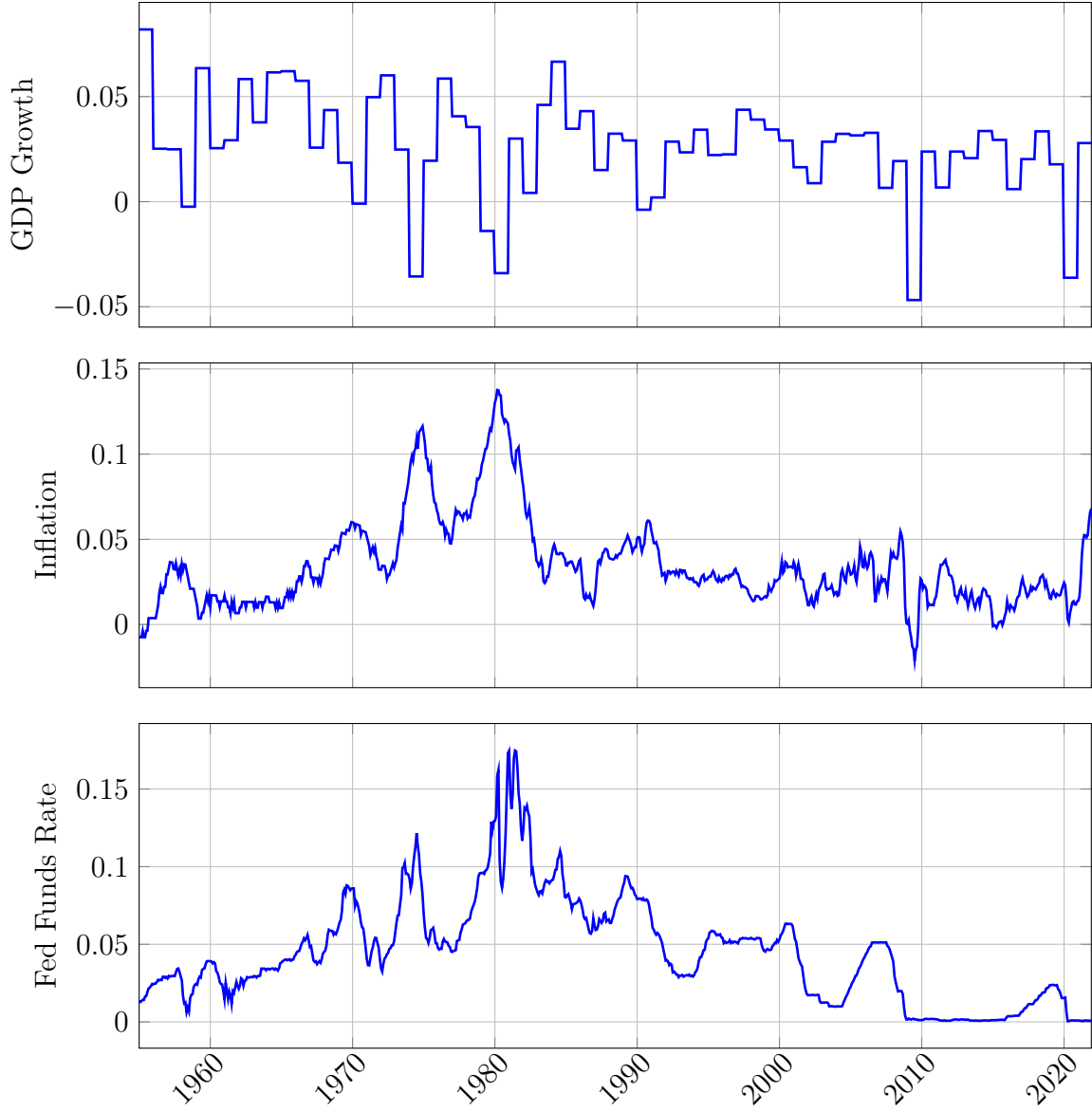
Turning now to stock market variance, the process (24) together with the log price-dividend ratio  $\Pi(x_t)$  imply the instantaneous stock return variance in this economy:

$$\sigma_t^2 = \sigma_D^2 + \sigma_\delta^2 \beta_\mu^2 \omega^2 \Pi_\phi^2 + \sigma_\pi^2 \Pi_\pi^2 - 2\lambda_\pi \nu_{a,t} \Pi_{\hat{a}} \Pi_\pi \phi_t + \frac{\lambda_\pi^2 \nu_{a,t}^2}{\sigma_\pi^2} \Pi_{\hat{a}}^2 \phi_t^2. \quad (28)$$

The last two terms in the stock return variance are novel, and are caused by the uncertainty about the Fed’s ability to control inflation. These terms show that the stock return variance increases when the Fed deviates from a neutral monetary policy ( $\phi_t \neq 0$ ). The term linear in  $\phi_t$  is positive during tightening episodes and negative during easing episodes, which creates an asymmetry that follows from the agent’s learning. As a result, we observe an asymmetric U-shaped pattern for stock return variance, with uncertainty about the Fed’s ability to control inflation becoming more important during tightening cycles.

### 3 Parameter Estimation

We estimate the model’s parameters by Maximum Likelihood using U.S. real Gross Domestic Product (GDP) data, Federal funds rate (Fed Funds rate) data, and Consumer Price Index (CPI) data. Appendix B provides details about the Maximum Likelihood estimation. Real GDP is from NIPA tables, while the Fed funds rate and the CPI are from FRED. The data is at the monthly frequency from January 1955 to December 2021. The log real GDP growth rate, log CPI growth rate, and continuously compounded Fed funds rate are used as proxies for the real log output growth rate  $\log(\delta_{t+\Delta}/\delta_t)$ , the inflation rate  $\pi_t$ , and the nominal interest rate  $r_{Nt}$ , respectively. These time series are depicted in Figure 1. The bottom panel reveals that the Federal funds rate exceeded 10% in the mid-1970s and early 1980s to combat soaring inflation, as shown in the middle panel. These elevated interest rates contributed to the economic downturns visible in the top panel of the figure.



**Figure 1: GDP Growth, Inflation, and Federal Funds Rate.**

This figure plots the observed annualized U.S. real GDP growth rate (top panel), CPI inflation rate (middle panel), and Federal Funds rate (bottom panel).

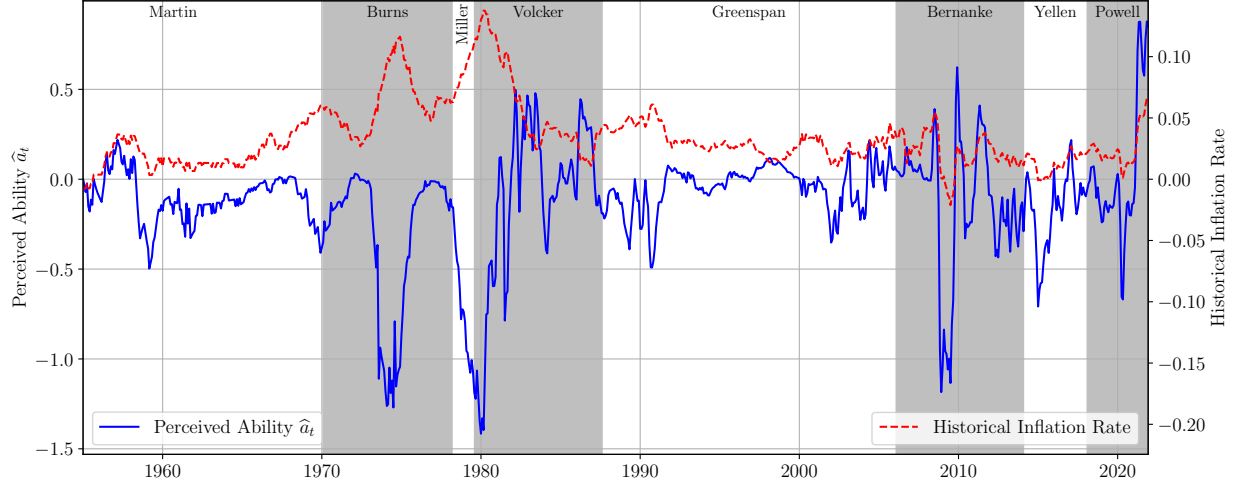
Table 1 presents the parameter values estimated using Maximum Likelihood. The estimated output gap and inflation coefficients  $\beta_\mu$  and  $\beta_\pi$  suggest that nominal interest rates respond more to inflation than to output growth (Clarida et al., 2000; Ang, Boivin, Dong, and Loo-Kung, 2011). The inflation and output growth indexes revert to their means at

Parameter	Symbol	Value
Output growth volatility	$\sigma_\delta$	0.0243*** (0.0005)
Mean inflation	$\bar{\pi}$	0.0345*** (0.0013)
Mean nominal interest rate	$\bar{r}_N$	0.0452*** (0.0009)
Mean-reversion speed of inflation index	$\omega_\pi$	0.4479*** (0.0364)
Mean-reversion speed of output growth index	$\omega_\mu$	0.4236*** (0.0455)
Interest rate sensitivity to inflation	$\beta_\pi$	1.3247*** (0.0310)
Interest rate sensitivity to output growth	$\beta_\mu$	1.0251*** (0.0790)
Inflation volatility	$\sigma_\pi$	0.0124*** (0.0002)
Mean inflation under neutral interest rates	$\check{\pi}$	0.0322*** (0.0030)
Mean-reversion speed of inflation	$\lambda_\pi$	0.6295*** (0.1240)
Volatility of the Fed's ability to control inflation	$\sigma_a$	0.8412*** (0.2763)
Mean-reversion speed of the Fed's ability to control inflation	$\lambda_a$	1.3149*** (0.4890)

**Table 1: Parameter values estimated by Maximum Likelihood.**

This table reports the parameter values estimated by Maximum Likelihood. The estimation procedure is detailed in Appendix B. The data is at the monthly frequency from January 1955 to December 2021. Output data is in real terms. Standard errors are reported in brackets, and statistical significance at the 10%, 5%, and 1% levels is denoted by \*, \*\*, and \*\*\*, respectively.

nearly identical rates,  $\omega_\pi$  and  $\omega_\mu$ . As a result, and in line with Section 2, we assume equal mean-reversion speeds:  $\omega_\pi = \omega_\mu \equiv \omega = 0.4479$ . Throughout our sample period, average inflation stands at 3.45%, and nominal interest rates at 4.52%, yielding an approximate average real interest rate of 1%. Notably, the historical average inflation rate is roughly 72% higher than the Fed's current 2% target, raising questions about the attainability and sustainability of this target.



**Figure 2: Agent’s perception of the Fed’s ability to control inflation.**

The figure juxtaposes the agent’s estimate of the Fed’s ability to control inflation,  $\hat{a}_t$  (solid line, left axis), with the historical inflation rate (dashed line, right axis). The alternating shaded bands mark the tenures of different Fed Chairpersons. The time series of  $\hat{a}_t$  is extracted from the Maximum Likelihood estimation.

Figure 2 plots the agent’s estimate of the Fed’s ability to control inflation (solid line, left axis) juxtaposed against the historical inflation rate (dashed line, right axis). Alternating shaded bands delineate the tenures of various Chairpersons at the Fed. Fed’s ability to control inflation,  $\hat{a}_t$ , varies substantially over the sample, suggesting shifting investors’ beliefs. A consistent pattern emerges when we consider inflation relative to its historical average. Specifically, when inflation is above this average, the correlation of changes in inflation with changes in  $\hat{a}_t$  is  $-0.4993$ . This suggests that an increase in inflation diminishes the perceived ability of the Fed. Conversely, when inflation falls below its historical mean, the correlation is  $0.6610$ . This dichotomy reflects the paper’s learning mechanism: both a spike in inflation during high inflationary periods and a decline during deflationary periods indicate to the agent that the Fed is losing its grip on inflation.

The time series of  $\hat{a}_t$  aligns with key historical periods. For instance, the ability to control inflation hit lows during the inflationary peaks of the mid-1970s and early 1980s. Yet, during Paul Volcker’s tenure (1979-1987),  $\hat{a}_t$  was consistently positive, resonating with his reputation for curbing that era’s inflation. Similarly, a positive ability marked Ben Bernanke’s term

(2006-2014), signifying his guidance during the global financial crisis.<sup>5</sup>

Figure 3 displays the historical paths of the tightening process  $\phi_t = r_{N,t} - \bar{r}_N$  (top panel) and the agent's long-term inflation expectation (bottom panel), defined in equation (6) and denoted as  $\hat{\pi}_t \equiv \bar{\pi} - \hat{a}_t(r_{N,t} - \bar{r}_N)$ . These time series result from the Maximum Likelihood estimation. The process  $\phi_t$  characterizes the Fed's tightening ( $\phi_t = r_{N,t} - \bar{r}_N > 0$ ) and easing ( $\phi_t = r_{N,t} - \bar{r}_N < 0$ ) cycles. The Fed tightened from late 1965 to early 1992 and eased from early 1955 to mid-1965, as well as from mid-1992 to late 2021. The Fed tightening index  $\phi_t$  exhibits a volatility of around 2.9% and an autocorrelation of approximately 0.996, indicating highly persistent tightening and easing cycles.

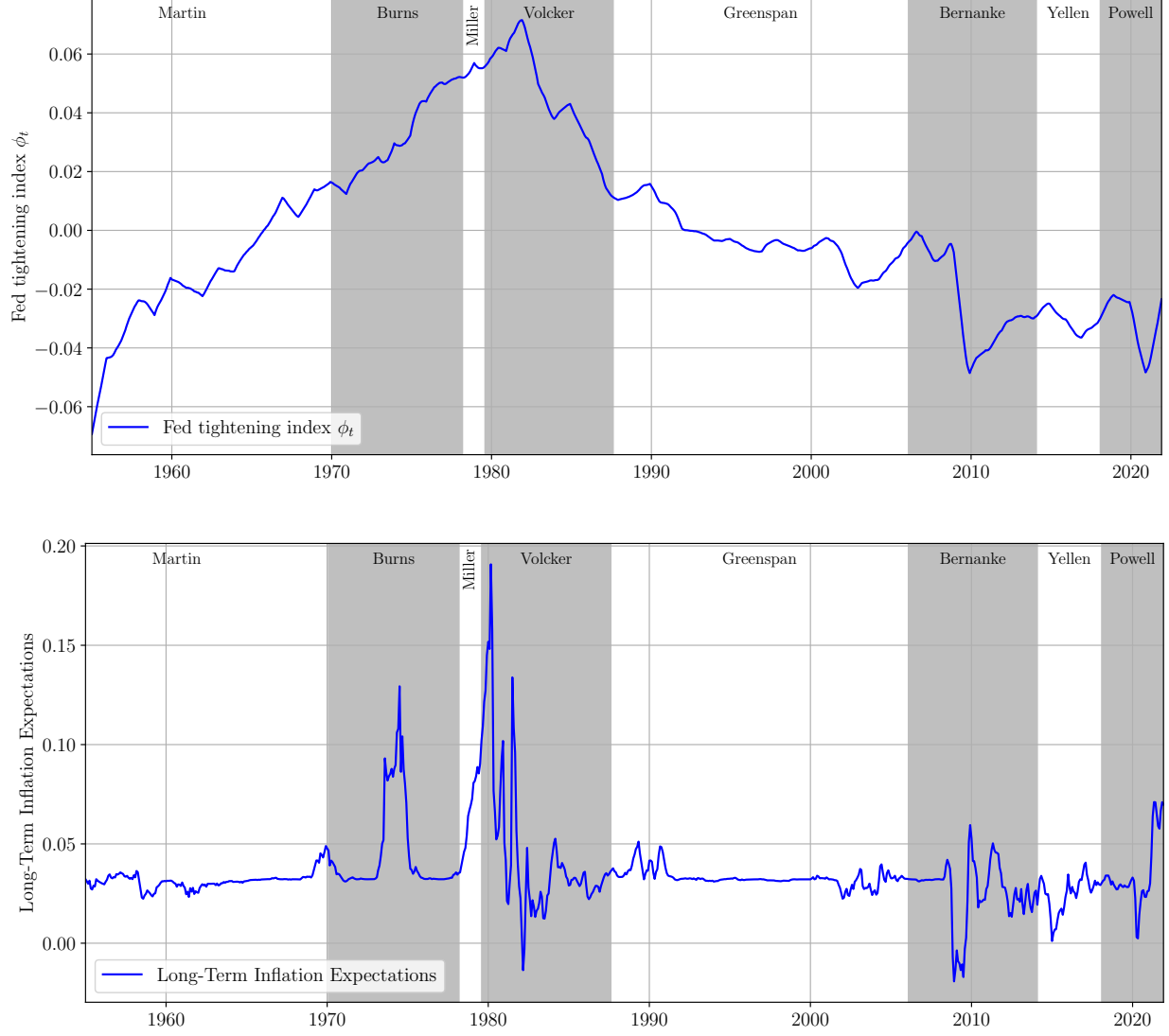
The bottom panel of Figure 3 plots the agent's long-term inflation expectation,  $\hat{\pi}_t \equiv \bar{\pi} - \hat{a}_t(r_{N,t} - \bar{r}_N)$ , which is driven by the agent's estimate of the Fed's ability to control inflation. The long-term inflation expectation has a volatility of 1.9% and an autocorrelation of 0.927, making it a relatively persistent process as well.<sup>6</sup> The long-term inflation expectation hits lows between -1.9% and 0% in early 1982 and late 2008 to mid-2009. The 1980-1982 recession lows followed the drastic interest rate increase implemented by the Paul Volcker-led Fed in mid-1981; the 2009 lows occurred at the end of the Great Recession, spurred by the subprime and financial crises. The highs range from 7% to 19% in mid-1973 to late 1974, mid-1979 to mid-1981, and mid to late 2021. The highs followed the 1973 oil crisis, during which Arab members of the Organization of Petroleum Exporting Countries (OPEC) imposed an oil embargo; and the most recent highs resulted from the unprecedented fiscal and monetary stimulus provided during the COVID-19 health crisis.

Consistent with the existing literature, we set the relative risk aversion, the elasticity of intertemporal substitution (EIS), subjective discount rate, dividend leverage on expected consumption growth, and dividend growth volatility to  $\gamma = 10$ ,  $\psi = 1.5$ ,  $\rho = 0.0045$ ,  $\alpha = 2.5$ , and  $\sigma_D = 0.05$ , respectively. As discussed later, these chosen parameter values, combined with the estimated parameters in Table 1 yield model-implied real interest rates, nominal

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<sup>5</sup>The spike in  $\hat{a}_t$  near the end of our sample (December 2021), during Jerome Powell's tenure, can be attributed to the Fed's easing stance coinciding with the onset of an inflationary uptrend. Given that inflation began to rise during this easing period, it appeared as though the Fed's actions were aligned with economic needs, in accordance with the learning process defined in (4).

<sup>6</sup>The agent's long-term inflation expectation,  $\hat{\pi}_t$ , has a 0.34 correlation with the median long-term annual average inflation over the next five years from the Survey of Professional Forecasters (SPF), available from the Federal Reserve Bank of Philadelphia since 2005Q3. Regressing the SPF's 5-year inflation forecast on  $\hat{\pi}_t$  yields a coefficient of 0.048 (t-stat = 2.9).



**Figure 3: Tightening cycles and long-term inflation expectations.**

This figure plots the Fed tightening index  $\phi_t = r_{N,t} - \bar{r}_N$  (top panel) and the agent's long-term inflation expectation (bottom panel), denoted as  $\hat{\pi}_t \equiv \bar{\pi} - \hat{a}_t(r_{N,t} - \bar{r}_N)$ . These time series are extracted from the Maximum Likelihood estimation.

interest rates, market risk premium, market return volatility, and market Sharpe ratio that reasonably match the data.

Table 2 presents asset-pricing moments, with the first column displaying empirical moments and the second column showing model-implied moments. We calculate empirical

<b>Moment</b>	<b>Data</b>	<b>Model</b>
Real interest rate	0.0105	0.0107
Nominal interest rate	0.0450	0.0453
Market risk premium	0.0605	0.0818
Market return volatility	0.1431	0.1896
Market Sharpe ratio	0.4228	0.4313

**Table 2: Asset-Pricing Moments.**

This table presents asset-pricing moments, with the first column displaying empirical moments and the second column showing model-implied counterparts. We calculate empirical moments using the Fed funds rate as the nominal interest rate, the difference between the Fed funds rate and the CPI inflation rate as the real interest rate, and the S&P 500 as the market. Model-implied moments are derived by inputting the state variable time series from the Maximum Likelihood estimation into the model. The data span monthly from January 1955 to December 2021.

moments using the Fed funds rate as the nominal interest rate, the difference between the Fed funds rate and the CPI inflation rate as the real interest rate, and the S&P 500 as the market. Model-implied moments are derived by inputting the state variable time series from the Maximum Likelihood estimation into the model. The model-implied real and nominal interest rates stand at 1% and 4.5%, respectively, aligning with their empirical counterparts. The model-implied market risk premium, market return volatility, and market Sharpe ratio are 8%, 19%, and 0.43, respectively. These values are reasonably close to their empirical counterparts, suggesting that the model generates realistic asset-pricing moments, even though our Maximum Likelihood estimation does not use any asset prices as inputs.

## 4 Results

In this section, we present the model’s predictions and subsequently offer empirical evidence to support them. All the illustrations are derived after solving the model using a numerical algorithm, which relies on the parameters estimated in Section 3. Details of the model



solution can be found in Appendix A.

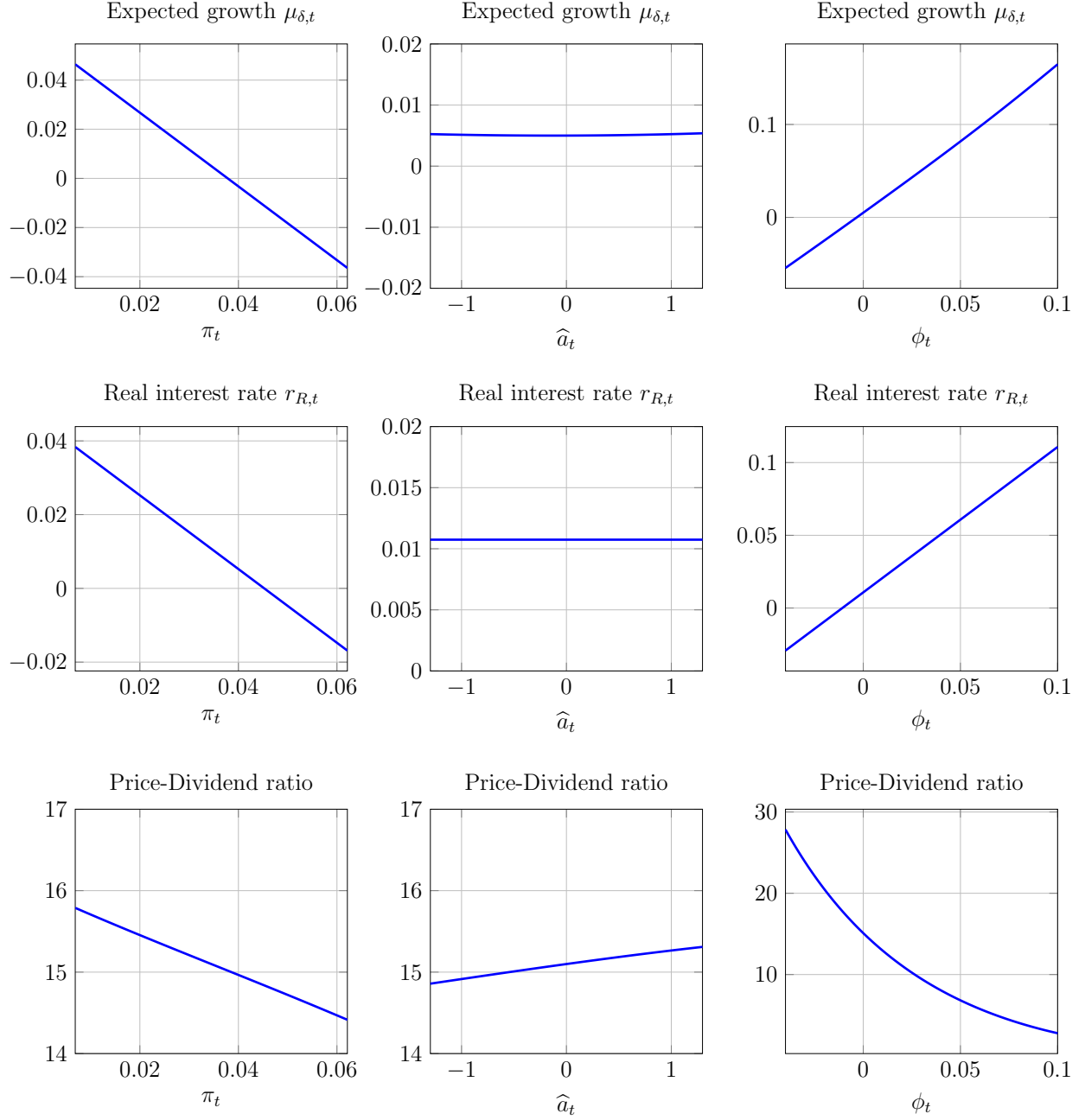
## 4.1 Model Predictions

Figure 4 illustrates the expected consumption growth  $\mu_{\delta,t}$ , the real interest rate  $r_{R,t}$ , and the log price-dividend ratio  $\Pi(x_t)$  as functions of the model's main state variables. The primary drivers of  $\mu_{\delta,t}$ ,  $r_{R,t}$ , and  $\Pi(x_t)$  are the expected inflation  $\pi_t$  and the Fed tightening index  $\phi_t$ . As a reminder, high values of  $\phi_t$  indicate tightening, while low values signify easing.

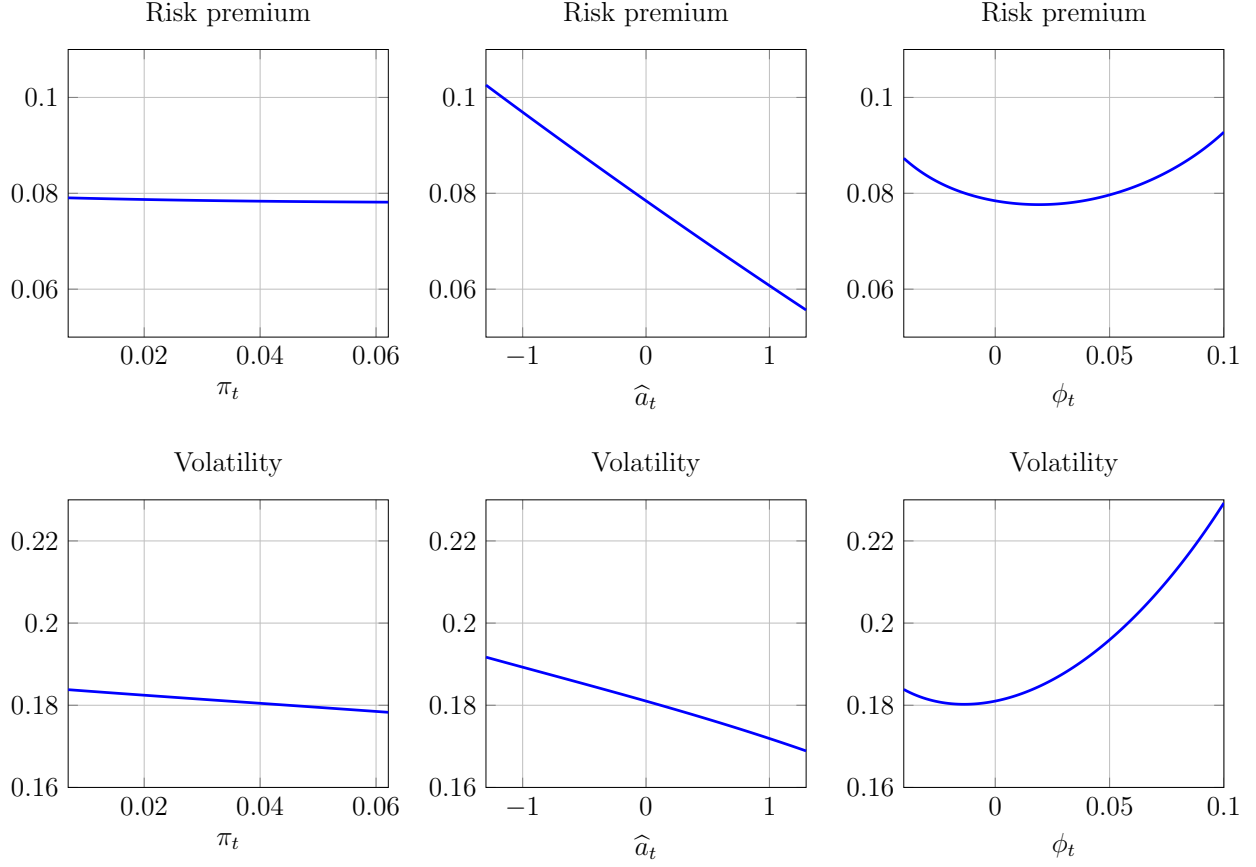
Figure 4 demonstrates that the expected consumption growth rate and the real interest rate decline as expected inflation increases. As shown in equation (22), equilibrium expected consumption growth is adversely impacted by inflation. High inflation encourages the agent to consume more today relative to tomorrow, reducing the expected consumption growth. Moreover, the Fisher Equation (7) suggests that when the nominal interest rate remains constant, an increase in expected inflation leads to a decrease in the real interest rate. Lastly, an increase in  $\phi_t$  results in monetary tightening and, via the Fisher equation (7), an increase in the real interest rate, which in turn leads to higher expected consumption growth as the agent optimally chooses to increase borrowing and delay consumption.

Shifting our attention to the price-dividend ratio (bottom panels), it decreases with expected inflation and the Fed tightening index  $\phi_t$  and increases with the Fed's perceived ability to control inflation  $\hat{a}_t$ . Thus, the inequalities conjectured in Section 2 ( $\Pi_\pi < 0$ ,  $\Pi_{\hat{a}} > 0$ , and  $\Pi_{\phi_\mu} < 0$ ) are now verified with our estimated parameter values.

The price-dividend ratio declines with expected inflation through equation (22), which demonstrates that the expected growth rate diminishes as expected inflation rises. This represents the pathway through which inflation introduces long-run risk into the economy. If the inflation process exhibits high persistence, an agent favoring early resolution of uncertainty will be averse to its fluctuations. The price-dividend ratio increases with the Fed's ability to control inflation because when  $\hat{a}_t$  is large and positive, the agent trusts that the Fed will promptly bring inflation back to its target, mitigating the long-run risk that it causes. Conversely, if  $\hat{a}_t$  is large and negative, the Fed will likely lose control of inflation, delaying its reversion to target and exacerbating long-run risk. Finally, the price-dividend ratio decreases with  $\phi_t$  because a high value for this variable signifies monetary tightening, leading to an increase in the discount rate through a rise in the real interest rate. Consequently, the



**Figure 4: Model Predictions** This figure plots the expected consumption growth  $\mu_{\delta,t}$ , the real interest rate  $r_{R,t}$ , and the price-dividend ratio as functions of the main state variables of the model. For this illustration, we have solved the model numerically (see Appendix A) using the parameters estimated in the Section 3.



**Figure 5: Model Predictions** This figure plots the risk premium and the stock market volatility as functions of the main state variables of the model. For this illustration, we have solved the model numerically (see Appendix A) using the parameters estimated in the Section 3.

price-dividend ratio falls when the Fed tightening index  $\phi_t$  increases.

Figure 5 displays the risk premium and stock market volatility as functions of the model's main state variables. The top three panels reveal that the risk premium is largely unresponsive to expected inflation but decreases significantly with the Fed's perceived ability to control inflation, as denoted by  $\hat{a}_t$ . This effect was discussed in relation to equation (27): since inflation is a source of long-run risk in this economy, the Fed's ability to revert it to its target holds value for the agent, lowering the risk premium as  $\hat{a}_t$  increases.

Figure 5 additionally reveals that the risk premium exhibits a U-shaped relationship with the Fed tightening index  $\phi_t$ . This arises from the uncertainty about the Fed's ability to

control inflation. In equation (27), the terms in the second row form a quadratic expression in  $\phi_t$ . Consequently, uncertainty about the Fed’s ability to control inflation amplifies the risk premium when the Fed deviates from a neutral monetary policy. Equation (27) also highlights an asymmetry, with the risk premium being higher during tightening; however, this effect is less pronounced with our estimated parameter values.

The bottom panels of Figure 5 depict the volatility of market returns as a function of the state variables, conveying a similar message to that of the risk premium: volatility is mostly unresponsive to expected inflation but decreases as the Fed’s ability to control inflation improves and increases with the Fed tightening index  $\phi_t$ . A notable distinction is the significant surge in volatility during tightening episodes, as shown in the bottom-right panel. This effect directly results from the term linear in  $\phi_t$  in equation (28): during a deep tightening cycle, inflation surprises are “doubled” by the agent’s learning process (an increase in inflation is doubly bad news, while a decrease is doubly good news). This intensifies the stock price’s sensitivity to inflation news, especially when the Fed embarks on aggressive tightening cycles.

## 4.2 Empirical Evidence

Does the data support our model’s predictions? To answer this question, we regress both the empirical and model-implied expected output growth rate, real interest rate, market price-dividend ratio, market risk premium, and market return volatility on the state variables. In other words, we verify and confirm that the data support the relationships depicted in Figures 4 and 5.

The *empirical* expected output growth rate, real interest rate, market price-dividend ratio, market risk premium, and market return volatility are obtained as follows:

- The empirical expected output growth rate is the fitted value of an ARMA(2,2) model applied to the realized GDP growth rate. In the estimation, the AR(1) and MA(2) coefficients are positive, whereas the AR(2) and MA(1) are negative. All coefficients are statistically significant at the 1% level, with the exception of the MA(1) coefficient, which is statistically significant at the 10% level.
- The empirical real interest rate is the difference between the Fed funds rate and the CPI inflation rate.

- The empirical market risk premium is the fitted value obtained by regressing the 1-year-ahead S&P 500 excess return on the current S&P 500 dividend yield (Fama and French, 1989; Cochrane, 2008) and realized S&P 500 return variance (French, Schwert, and Stambaugh, 1987; Guo, 2006).<sup>7</sup> In the predictive regression, both the dividend yield and realized variance load positively and significantly at the 5% level and 1% level, respectively.
- The empirical market return volatility is obtained by fitting an Exponential GARCH(1,1) model (Nelson, 1991) on the S&P 500 excess return residual,<sup>8</sup> where the return residual is the difference between the S&P 500 excess return and the empirical risk premium. The ARCH(1) and GARCH(1) coefficients are positive and statistically significant at the 1% level, and the LEVERAGE(1) coefficient is negative and statistically significant at the 1% level.

The *model-implied* expected output growth rate, real interest rate, market price-dividend ratio, market risk premium, and market return volatility are obtained by feeding the model with the state variables extracted from the Maximum Likelihood estimation performed in Section 3.

Table 3 documents the relationships between the empirical moments and their model-implied counterparts by reporting the outputs of regressing the empirical moments on their model-implied counterparts. All relations are positive, statistically significant at the 1% level, and feature high  $R^2$ s. The explanatory power of the model-implied moments is particularly high for the risk premium, log price-dividend ratio, and real interest rate. Indeed, the model-implied risk premium, log price-dividend ratio, and real interest rate explain respectively 20.6%, 40.4%, and 44.8% of the variation in their empirical counterparts. These results show that the dynamics of the model-implied moments align with the dynamics of the empirical moments, and that the model-implied moments explain a substantial fraction of the variation in the empirical moments. To summarize, the model describes the observed dynamics of asset prices well, and this despite the fact that the Maximum Likelihood estimation used to infer model-implied moments does not use any asset prices as inputs.

We now test the relationships depicted in Figure 4. Table 4 reports the empirical and

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<sup>7</sup>S&P 500 returns, dividend yield, and realized variance are obtained from Amit Goyal's website.

<sup>8</sup>The Exponential GARCH model accounts for the asymmetric response of volatility to return shocks.

	Expected output growth	Real interest rate	Log price-div. ratio	Risk premium	Volatility
$\mu_{\delta,t}$	0.084*** (9.864)				
$r_{R,t}$		0.790*** (5.649)			
$pd_t$			0.485*** (4.157)		
$RP_t$				1.687*** (6.332)	
$Vol_t$					0.318*** (8.300)
$R^2$	0.099	0.448	0.404	0.206	0.036
Obs.	804	804	804	804	804

**Table 3: Empirical Moments vs. Model-Implied Counterparts.**

This table reports the outputs obtained by regressing the empirical moments on their model-implied counterparts.  $t$ -statistics are in brackets and are computed using [Newey and West \(1987\)](#)-adjusted standard errors. Statistical significance at the 1%, 5%, and 10% levels are denoted by \*\*\*, \*\*, and \*, respectively. The data are at the monthly frequency from January 1955 to December 2021.

model-implied relations between the state variables and the expected output growth rate  $\mu_{\delta,t}$ , real interest rate  $r_{R,t}$ , and log price-dividend ratio  $\Pi(x_t)$ . As Figure 4 shows, the main drivers of  $\mu_{\delta,t}$ ,  $r_{R,t}$ , and  $\Pi(x_t)$  are the Fed tightening index  $\phi_t$  and inflation  $\pi_t$ , which the “Model”-labeled columns in Table 4 confirm. Indeed, the Fed tightening index and inflation explain more than 99% of the variation in  $\mu_{\delta,t}$ ,  $r_{R,t}$ , and  $\Pi(x_t)$ . The “Data”-labeled columns confirm these relations. The expected output growth rate and the real interest rate increase with the Fed tightening index and decrease with inflation, with statistically significant slopes at the 1% level. This occurs because an increase in  $\phi_t$  leads to monetary tightening, causing the nominal interest rate to rise through the Fed’s Taylor rule (15). The Fisher equation (7) then implies that the real interest rate rises with the Fed tightening index  $\phi_t$  and decreases with inflation  $\pi_t$ . Furthermore, the equilibrium relation (21) implies that the real interest rate depends linearly on the expected output growth rate. Thus,  $\phi_t$  and  $\pi_t$  drive the expected

	Expected output growth		Real interest rate		Log price-dividend ratio	
	Model	Data	Model	Data	Model	Data
$\phi_t$	1.498*** (> 100)	0.106*** (8.125)	1.000*** (> 100)	0.812*** (5.253)	-15.581*** (< -100)	-7.544*** (-2.694)
$\pi_t$	-1.489*** (< -100)	-0.175*** (-8.272)	-1.000*** (< -100)	-0.732*** (-9.055)	-2.787*** (-24.163)	-1.198 (-0.968)
$R^2$	0.999	0.152	1.000	0.456	0.997	0.391
Obs.	804	804	804	804	804	804

**Table 4: Expected Output Growth, Real Interest Rate, and Log Price-Dividend Ratio vs. State Variables.**

This table reports the model-implied and empirical relations between the expected real output growth rate, real interest rate, log price-dividend ratio, and their drivers. The drivers are the Fed tightening index  $\phi_t$  and inflation  $\pi_t$ .  $t$ -statistics are in brackets and are computed using Newey and West (1987)-adjusted standard errors. Statistical significance at the 1%, 5%, and 10% levels are denoted by \*\*\*, \*\*, and \*, respectively. The data are at the monthly frequency from January 1955 to December 2021.

output growth rate in the same direction they drive the real interest rate.

Table 4 further shows that the price-dividend ratio decreases significantly with the Fed tightening index  $\phi_t$ , both in the model and in the data. An increase in  $\phi_t$  raises discount rates through tightening. As a result, prices drop as the Fed tightening index rises. Furthermore, both the model-implied and empirical price-dividend ratios decrease with inflation, although the empirical relation is not statistically significant. A rise in inflation implies a decrease in expected output growth and, therefore, in expected dividend growth, leading to a lower price-dividend ratio.

Table 5 presents the empirical and model-implied relations between the market risk premium (Panel A), market return volatility (Panel B), and their primary drivers. As shown in Figure 5, the key drivers include the Fed’s ability to control inflation  $\hat{a}_t$ , the Fed tightening index  $\phi_t$ , and the squared Fed tightening index  $\phi_t^2$ . The “Model”-labeled columns in Table 5 support this observation. These three state variables explain over 86% of the variation in the market risk premium and market return volatility. In both the model and data, an increase in the Fed’s ability to control inflation significantly reduces the market risk premium and market return volatility. As the Fed’s inflation control ability improves, the likelihood of

Panel A: Risk premium vs. state variables				
	Risk premium		Risk premium	
	Model	Data	Model	Data
$\hat{a}_t$	-0.012*** (-9.988)	-0.017*** (-3.581)	-0.011*** (-9.701)	-0.016*** (-3.329)
$\phi_t$	0.104*** (4.508)	0.275*** (3.964)	0.070*** (4.728)	0.224*** (2.724)
$\phi_t^2$			2.408*** (6.147)	3.641*** (2.914)
$R^2$	0.721	0.205	0.863	0.228
Obs.	804	804	804	804

Panel B: Return volatility vs. state variables				
	Volatility		Volatility	
	Model	Data	Model	Data
$\hat{a}_t$	-0.014*** (-6.288)	-0.034*** (-6.700)	-0.011*** (-6.406)	-0.034*** (-6.569)
$\phi_t$	0.632*** (10.150)	0.151*** (5.610)	0.509*** (13.161)	0.173*** (7.642)
$\phi_t^2$			8.715*** (6.228)	-1.518 (-1.628)
$R^2$	0.745	0.101	0.884	0.102
Obs.	804	804	804	804

**Table 5: Market Risk Premium and Return Volatility vs. State Variables.**

This table reports the model-implied and empirical relations between the market risk premium (Panel A), market return volatility (Panel B), and their drivers. The drivers are the Fed’s ability to control inflation  $\hat{a}_t$ , the Fed tightening index  $\phi_t$ , and the squared Fed tightening index  $\phi_t^2$ .  $t$ -statistics are in brackets and are computed using [Newey and West \(1987\)](#)-adjusted standard errors. Statistical significance at the 1%, 5%, and 10% levels are denoted by \*\*\*, \*\*, and \*, respectively. The data are at the monthly frequency from January 1955 to December 2021.

encountering high future inflation during tightening (or low future inflation during easing) diminishes (refer to equation (6)). In other words, the Fed reduces the persistence of inflation and the associated long-run risk, which consequently leads to a lower market risk premium and decreased market return volatility in equilibrium.



Moreover, both in the model and the data, the market risk premium and market return volatility significantly increase with the Fed tightening index  $\phi_t$ . As previously mentioned, inflation surprises are amplified during tightening through investor learning. For example, a positive inflation surprise during tightening is doubly bad news because it weakens the agent’s confidence in the Fed; in contrast, the same inflation surprise during easing is good news, as it boost the Fed’s credibility. This asymmetry contributes to a higher market risk premium and market return volatility during tightening episodes.

Lastly, in the model, the market risk premium and market return volatility increase significantly with the squared Fed tightening index. This quadratic relationship stems from the last term in equations (27) and (28), where  $(r_{N,t} - \bar{r}_N)^2 = \phi_t^2$ , and arises due to uncertainty surrounding the Fed’s ability to control inflation. The data confirm the positive impact of the squared Fed tightening index on the market risk premium, with a statistically significant relationship at the 1% level. However, the data reveal no significant empirical correlation between the market return volatility and the squared Fed tightening index.

Table 6 reports the relations between the market risk premium and the market log price-dividend ratio (Panel A), the expected real output growth (Panel B), and the real interest rate (Panel C) both in the model and in the data. Panel A shows that the market price-dividend ratio negatively and significantly predicts the market risk premium both in the model and in the data, in line with [Boudoukh, Michaely, Richardson, and Roberts \(2007\)](#), [Cochrane \(2008\)](#), and [van Binsbergen and Koijen \(2010\)](#). When controlling for inflation  $\pi_t$  and the Fed’s ability to control inflation  $\hat{a}_t$ , the risk premium’s negative loading on the market price-dividend ratio remains statistically significant at the 1% level. The loading on inflation is statistically insignificant, and the negative loading on the Fed’s ability to control inflation is statistically significant at the 1% level.

Panel B shows that, both in the model and in the data, there is no statistically significant relation between the market risk premium and the expected output growth rate when the regression does not feature any control. However, in line with the empirical findings of [Fama \(1981\)](#) and [Fama \(1990\)](#), the relation between the market risk premium and the expected output growth rate becomes positive and highly statistically significant when controlling for inflation and the Fed’s ability to control inflation. Similarly, Panel C shows that, both in the model and in the data, the positive relation between the market risk premium and the real interest rate strengthens significantly when controlling for inflation and the Fed’s ability

Panel A: Risk premium vs. price-dividend ratio

	Risk premium		Risk premium		Risk premium	
	Model	Data	Model	Data	Model	Data
$pd_t$	-0.008*** (-5.864)	-0.039*** (-41.488)	-0.005*** (-4.829)	-0.039*** (-15.897)	-0.006*** (-4.308)	-0.038*** (-25.738)
$\pi_t$			0.069 (1.410)	0.007 (0.164)	-0.001 (-0.075)	-0.022 (-0.626)
$\hat{a}_t$					-0.012*** (-7.804)	-0.008*** (-3.028)
$R^2$	0.437	0.430	0.464	0.430	0.740	0.441
Obs.	804	804	804	804	804	804

Panel B: Risk premium vs. expected output growth

	Risk premium		Risk premium		Risk premium	
	Model	Data	Model	Data	Model	Data
$\mu_{\delta,t}$	0.018 (0.711)	-0.031 (-0.372)	0.048*** (4.416)	0.298*** (3.361)	0.060*** (4.086)	0.254*** (2.784)
$\pi_t$			0.163*** (4.907)	0.329*** (8.101)	0.112*** (4.782)	0.257*** (6.140)
$\hat{a}_t$					-0.012*** (-7.240)	-0.015* (-1.686)
$R^2$	0.007	0.000	0.451	0.125	0.727	0.158
Obs.	804	804	804	804	804	804

Panel C: Risk premium vs. real interest rate

	Risk premium		Risk premium		Risk premium	
	Model	Data	Model	Data	Model	Data
$r_{R,t}$	0.0241 (0.616)	0.154** (2.413)	0.070*** (4.396)	0.172*** (4.332)	0.089*** (4.019)	0.178*** (4.924)
$\pi_t$			0.163*** (4.912)	0.311*** (8.181)	0.113*** (4.739)	0.239*** (7.229)
$\hat{a}_t$					-0.012*** (-7.165)	-0.016** (-2.253)
$R^2$	0.005	0.022	0.449	0.144	0.725	0.181
Obs.	804	804	804	804	804	804

**Table 6: Market Risk Premium vs. Market Price-Dividend Ratio, Expected Output Growth, and Real Interest Rate.**

This table reports the model-implied and empirical relations between the market risk premium and market log price-dividend ratio  $pd_t$  (panel A), expected real output growth rate  $\mu_{\delta,t}$  (Panel B), and real interest rate  $r_{R,t}$  (Panel C) controlling for inflation  $\pi_t$  and the Fed's ability to control inflation  $\hat{a}_t$ .  $t$ -statistics are in brackets and are computed using Newey and West (1987)-adjusted standard errors. Statistical significance at the 1%, 5%, and 10% levels are denoted by \*\*\*, \*\*, and \*, respectively. The data are at the monthly frequency from January 1955 to December 2021.

to control inflation. These results highlight the importance of controlling for inflation and the Fed’s ability to control inflation to highlight the predictive power of the market price-dividend ratio, expected output growth rate, and real interest rate for future excess market returns.<sup>9</sup>

Overall, this section shows that the relations between asset-pricing moments and economic fundamentals predicted by the model are confirmed by the data. The market risk premium and return volatility decrease with the Fed’s ability to control inflation, and increase (quadratically) when the Fed tightens financial conditions. Furthermore, the expected output growth, real interest rate, and market price-dividend ratio decrease with inflation. As financial conditions get tighter, the price-dividend ratio drops and both the expected output growth and real interest rate increase.

## 5 Conclusion

This paper examines how the market perceives the Fed’s ability to control inflation. Investors infer the success of the Fed’s actions from inflation data, which has stock market implications. When the Fed’s credibility is strong, market risk premiums and volatility decline. Conversely, when investors doubt the Fed’s ability to control inflation, these financial measures increase, potentially causing a significant stock market downturn. Empirical evidence supports these theoretical predictions, highlighting the role of the market’s perception of the Fed’s inflation-fighting efforts on stock market dynamics.

The Fed has developed effective tools to address inflation by building on experiences from the 1970s’ Great Inflation, increased policy autonomy, and a more comprehensive grasp of inflation causes and countermeasures. Among these tools, our paper argues that credibility in combating inflation may be the Fed’s most valuable asset. This credibility is intrinsically tied to investors’ confidence in the Fed’s ability and the importance of a solid reputation in managing monetary policy effectively.

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<sup>9</sup>The relationship among stock returns, interest rates, and inflation has been extensively debated in the literature, yielding mixed evidence. [Fama and Schwert \(1977\)](#) and [Campbell \(1987\)](#) show that there is a negative relationship between market returns and nominal interest rates. However, [Campbell and Ammer \(1993\)](#) document a positive, albeit weak, relationship between market returns and real interest rates. The relationship between market returns and inflation is debated in [Fama and Schwert \(1977\)](#), [Fama \(1981\)](#), [Geske and Roll \(1983\)](#), and [Kaul \(1987\)](#), while the interplay between expected returns and output growth is explored by [Fama \(1981, 1990\)](#) and [Ritter \(2005\)](#).

Furthermore, this paper emphasizes the importance of investors' responses to the Fed's actions as a critical economic factor. While our study does not explore the impact of fluctuating investors' attention, it is plausible that heightened uncertainty—particularly during aggressive tightening where inflation shocks are “doubled” by the learning-induced asymmetric effect—could lead to increased attention to news, intensifying the observed effects (Kroner, 2023; Pfäuti, 2023). Future research might also investigate how heterogeneous investor beliefs about the Fed's ability to manage inflation affect markets, evaluate how the swift pace of our information age impacts investor learning about the Fed, and perform comparative international analyses to provide additional empirical validation of these findings. A deeper exploration in these areas is vital to understand the impact of monetary policy on the stock market and the economy.

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# Appendix

## A Details on Model Resolution in Section 2

**Learning:** To obtain the agent's posterior mean  $\hat{a}_t \equiv \mathbb{E}[a_t | \mathcal{F}_t^{\pi, r_N}]$  and the posterior variance  $\nu_{a,t} \equiv \mathbb{E}[(a_t - \hat{a}_t)^2 | \mathcal{F}_t^{\pi, r_N}]$  as in (4)-(5), apply Theorem 12.7 in [Liptser and Shiryaev \(2001\)](#) with:

$$\begin{aligned} A_0 &= \lambda_\pi(\check{\pi} - \pi_t), & A_1 &= -\lambda_\pi(r_{N,t} - \bar{r}_N), & B_1 &= 0, & B_2 &= [0 \ \sigma_\pi], \\ a_0 &= \lambda_a \bar{a}, & a_1 &= -\lambda_a, & b_1 &= \sigma_a, & b_2 &= [0 \ 0]. \end{aligned}$$

The surprise change in expected inflation according to the agent's information set  $\mathcal{F}^\pi$  is

$$d\hat{B}_{\pi,t} = dB_{\pi,t} + \frac{\lambda_\pi}{\sigma_\pi}(\hat{a}_t - a_t)(r_{N,t} - \bar{r}_N)dt.$$

**HJB equation:** The partial differential equation (PDE) that results from (16)-(17) is:

$$\begin{aligned} 0 &= e^{-I} - \rho + \frac{\gamma - 1}{\theta} \left( \frac{\gamma \sigma_\delta^2}{2} - \mu_{\delta,t} \right) + \lambda_\pi [\hat{a}_t(\bar{r}_N - r_{N,t}) + \check{\pi} - \pi_t] I_\pi - \lambda_a \hat{a}_t I_{\hat{a}} \\ &+ \omega [\beta_\pi(\pi_t - \bar{\pi}) + \beta_\mu(\mu_{\delta,t} - \bar{\mu}_\delta) - \phi_t - \beta_\mu(\gamma - 1)\sigma_\delta^2] I_\phi \\ &+ \frac{\sigma_\pi^2}{2} I_{\pi\pi} + \frac{(\bar{r}_N - r_{N,t})^2 \lambda_\pi^2 \check{\nu}_a^2}{2\sigma_\pi^2} I_{\hat{a}\hat{a}} + \frac{\sigma_\delta^2 \beta_\mu^2 \omega^2}{2} I_{\phi\phi} + (\bar{r}_N - r_{N,t}) \lambda_\pi \check{\nu}_a I_{\pi\hat{a}} \\ &+ \frac{\theta \sigma_\pi^2}{2} I_\pi^2 + \frac{\theta(\bar{r}_N - r_{N,t})^2 \lambda_\pi^2 \check{\nu}_a^2}{2\sigma_\pi^2} I_{\hat{a}}^2 + \frac{\theta \sigma_\delta^2 \beta_\mu^2 \omega^2}{2} I_\phi^2 + \theta(\bar{r}_N - r_{N,t}) \lambda_\pi \check{\nu}_a I_\pi I_{\hat{a}}. \end{aligned}$$

To derive this PDE, we set  $\nu_{a,t} = \check{\nu}_a$ , which removes one state variable and simplifies the numerical solution process. It is important to note that the theoretical results stated in Section 2 are not affected by this assumption. Moreover, our numerical analysis of the model with a time-varying  $\nu_{a,t}$  showed that the price-dividend ratio barely changes in response to  $\nu_{a,t}$ , although the solution process becomes significantly slower. Consequently, we decided to use a fixed  $\nu_{a,t} = \check{\nu}_a$ .

The PDE for  $I(\pi_t, \hat{a}, \phi)$  is solved numerically using the Chebyshev collocation method ([Judd, 1998](#)). That is, we approximate the function  $I(\pi_t, \hat{a}, \phi)$  as follows:

$$I(\pi_t, \hat{a}, \phi) \approx \mathcal{P}(\pi_t, \hat{a}, \phi) = \sum_{i=0}^I \sum_{j=0}^J \sum_{k=0}^K a_{i,j,k} T_i[\pi] \times T_j[\hat{a}] \times T_k[\phi],$$

where  $T_m[\cdot]$  is the Chebyshev polynomial of order  $m$ . The interpolation nodes are obtained by meshing the scaled roots of the Chebyshev polynomials of order  $I + 1$ ,  $J + 1$ , and  $K + 1$ . We scale the roots of the Chebyshev polynomials such that they cover approximately 99% of the unconditional distributions of the three state variables (which are all mean-reverting).

The polynomial  $\mathcal{P}(\pi_t, \hat{a}, \phi)$  and its partial derivatives are then substituted into the PDE, and the resulting expression is evaluated at the interpolation nodes. This yields a system of  $(I + 1) \times$

$(J+1) \times (K+1)$  equations with  $(I+1) \times (J+1) \times (K+1)$  unknowns (the coefficients  $a_{i,j,k}$ ). This system of equations is solved numerically.

To verify the solution method's accuracy and address potential concerns about anomalous numerical outcomes, we employed two distinct platforms (Mathematica and Python) and multiple grid dimensions for solving the PDE. In all cases, the results were consistently similar, reinforcing the method's reliability.

Finally, the PDE for the log price dividend ratio  $\Pi_t$  of the asset that is a claim to the dividend process (24) is given by:

$$\begin{aligned}
0 = & e^{-\Pi} - \rho + \frac{\gamma\sigma_\delta^2(\psi+1)}{2\psi} + (1-\alpha)\bar{\mu}_\delta + \left(\alpha - \frac{1}{\psi}\right)\mu_{\delta,t} + \lambda_\pi[\hat{a}_t(\bar{r}_N - r_{N,t}) + \check{\pi} - \pi_t]\Pi_\pi \\
& - \lambda_a\hat{a}_t\Pi_{\hat{a}} + \omega[\beta_\pi(\pi_t - \bar{\pi}) + \beta_\mu(\mu_{\delta,t} - \bar{\mu}_\delta) - \phi_t - \beta_\mu\gamma\sigma_\delta^2]\Pi_\phi + \frac{\sigma_\pi^2}{2}\Pi_{\pi\pi} + \frac{(\bar{r}_N - r_{N,t})^2\lambda_\pi^2\check{\nu}^2}{2\sigma_\pi^2}\Pi_{\hat{a}\hat{a}} \\
& + \frac{\sigma_\delta^2\beta_\mu^2\omega^2}{2}\Pi_{\phi\phi} + (\bar{r}_N - r_{N,t})\lambda_\pi\check{\nu}\Pi_{\pi\hat{a}} - (\theta-1)\sigma_\delta^2\beta_\mu\omega I_\phi + \frac{\sigma_\pi^2}{2}\Pi_\pi^2 + (\bar{r}_N - r_{N,t})\lambda_\pi\check{\nu}\Pi_\pi\Pi_{\hat{a}} \\
& + (\theta-1)\sigma_\pi^2\Pi_\pi I_\pi + (\theta-1)(\bar{r}_N - r_{N,t})\lambda_\pi\check{\nu}\Pi_\pi I_{\hat{a}} + (\theta-1)(\bar{r}_N - r_{N,t})\lambda_\pi\check{\nu}\Pi_{\hat{a}} I_\pi \\
& + \frac{(\bar{r}_N - r_{N,t})^2\lambda_\pi^2\check{\nu}^2}{2\sigma_\pi^2}\Pi_{\hat{a}}^2 + \frac{(\theta-1)(\bar{r}_N - r_{N,t})^2\lambda_\pi^2\check{\nu}^2}{\sigma_\pi^2}\Pi_{\hat{a}} I_{\hat{a}} + \frac{\sigma_\delta^2\beta_\mu^2\omega^2}{2}\Pi_\phi^2 + (\theta-1)\sigma_\delta^2\beta_\mu^2\omega^2\Pi_\phi I_\phi \\
& - \frac{\theta-1}{2}\sigma_\pi^2 I_\pi^2 - (\theta-1)(\bar{r}_N - r_{N,t})\lambda_\pi\check{\nu} I_\pi I_{\hat{a}} - \frac{(\theta-1)(\bar{r}_N - r_{N,t})^2\lambda_\pi^2\check{\nu}^2}{2\sigma_\pi^2} I_{\hat{a}}^2 - \frac{1}{2}(\theta-1)\sigma_\delta^2\beta_\mu^2\omega^2 I_\phi^2.
\end{aligned}$$

We replace the solution for the log-wealth consumption ratio  $I$  in the above PDE, then solve for the log price-dividend ratio  $\Pi$  using the same numerical procedure.

## B Maximum Likelihood Estimation in Section 3

U.S. GDP is from NIPA tables. Real values are used as proxies for the output  $\delta_t$  and dividend  $D_t$ . The Fed funds rate is from FRED, and its annualized continuously compounded value is used as proxy for nominal risk-free rate  $r_{Nt}$ . The year-over-year log growth rate of the Consumer Price Index (CPI) is the proxy for  $\pi_t$ . Time series are at the monthly frequency from January 1955 to December 2021.

The GDP growth rate volatility is obtained by maximizing the following log-likelihood function

$$l_\delta(\Theta_\delta; u_{\delta,\Delta}, \dots, u_{\delta,J\Delta}) = \sum_{j=1}^J \log \left( \frac{1}{(2\pi)^{1/2} \sqrt{\sigma_\delta^2 \Delta}} \right) - \frac{1}{2} (\sigma_\delta^2 \Delta)^{-1} u_{\delta,j\Delta}^2,$$

where  $\Delta = 1/12$ ,  $\Theta_\delta \equiv (\sigma_\delta)^T$ ,  $J$  is the number of observations,  $\top$  is the transpose operator, and

$$u_{\delta,t+\Delta} = \log(\delta_{t+\Delta}/\delta_t) - \left( \text{avg(GDP growth)} - \frac{1}{2}\sigma_\delta^2 \right) \Delta.$$

avg(GDP growth) stands for the annualized empirical average of the GDP growth rate.

The unconditional mean of inflation is obtained by maximizing the following log-likelihood function

$$l_p(\Theta_p; u_{p,\Delta}, \dots, u_{p,J\Delta}) = \sum_{j=1}^J \log \left( \frac{1}{(2\pi)^{1/2} \sqrt{\text{var}(\text{inflation})\Delta}} \right) - \frac{1}{2} (\text{var}(\text{inflation})\Delta)^{-1} u_{p,j\Delta}^2,$$

where  $\Delta = 1/12$ ,  $\Theta_p \equiv (\bar{\pi})^\top$ ,  $J$  is the number of observations,  $\top$  is the transpose operator, and

$$u_{p,t} = \pi_t - \bar{\pi}\Delta.$$

var(inflation) stands for the annualized empirical variance of inflation.

The parameters driving the Taylor rule are obtained by maximizing the following log-likelihood function

$$l_r(\Theta_r; u_{r,\Delta}, \dots, u_{r,J\Delta}) = \sum_{j=1}^J \log \left( \frac{1}{(2\pi)^{1/2} \sqrt{\sigma_r^2 \Delta}} \right) - \frac{1}{2} (\sigma_r^2 \Delta)^{-1} u_{r,j\Delta}^2,$$

where  $\Theta_r \equiv (\bar{r}_N, \omega_\pi, \omega_\mu, \beta_\pi, \beta_\mu, \sigma_r)^\top$  and

$$u_{r,t} = r_{Nt} - [\bar{r}_N + \beta_\mu (\phi_{\mu,t} - \text{avg}(\text{GDP growth})) + \beta_\pi (\phi_{\pi,t} - \text{avg}(\text{Inflation}))].$$

The annualized empirical averages of the Fed funds rate, GDP growth rate, and inflation rate are denoted by avg(Fed funds), avg(GDP growth), and avg(Inflation), respectively. The performance indices  $\phi_{\mu,t}$  and  $\phi_{\pi,t}$  are obtained by discretizing the dynamics in (10) and (9) as follows

$$\begin{aligned} \phi_{\mu,t} &= \omega_\mu \sum_{k=0}^K e^{-\omega_\mu k \Delta} \log(\delta_{t-k\Delta} / \delta_{t-(k+1)\Delta}), \\ \phi_{\pi,t} &= \omega_\pi \sum_{k=0}^K e^{-\omega_\pi k \Delta} \pi_{t-k\Delta} \Delta, \end{aligned}$$

where  $K$  is the number of observations prior to time  $t$ .

To obtain the parameters driving inflation, we discretize the solutions of the stochastic differential equations in (6) and (4) as follows

$$\begin{aligned} \pi_{t+\Delta} &= \pi_t e^{-\lambda_\pi \Delta} + \hat{\pi}_t (1 - e^{-\lambda_\pi \Delta}) + \sqrt{\text{var}_\pi} \epsilon_{\pi,t+\Delta}, \\ \hat{\pi}_t &= \check{\pi} - \hat{a}_t (r_{Nt} - \bar{r}_N) \\ \hat{a}_{t+\Delta} &= \hat{a}_t e^{-\lambda_a \Delta} - \frac{(r_{Nt} - \bar{r}_N) \lambda_\pi \nu_{a,t}}{\sigma_\pi} \sqrt{\frac{1 - e^{-2\lambda_a \Delta}}{2\lambda_a}} \epsilon_{\pi,t+\Delta}, \end{aligned} \tag{B29}$$

$$\nu_{a,t+\Delta} = \nu_{a,t} + \left[ \sigma_a^2 - 2\lambda_a \nu_{a,t} - \left( \frac{(r_{Nt} - \bar{r}_N) \lambda_\pi \nu_{a,t}}{\sigma_\pi} \right)^2 \right] \Delta, \quad (\text{B30})$$

where  $var_\pi = \frac{\sigma_\pi^2}{2\lambda_\pi} (1 - e^{-2\lambda_\pi \Delta})$  and  $\epsilon_{\pi,t+\Delta}$  is a normally distributed random variable with mean zero and variance one. The parameters driving inflation are obtained by maximizing the following log-likelihood function

$$l_\pi(\Theta_\pi; u_{\pi,\Delta}, \dots, u_{\pi,J\Delta}) = \sum_{j=1}^J \log \left( \frac{1}{(2\pi)^{1/2} \sqrt{var_\pi}} \right) - \frac{1}{2} (var_\pi)^{-1} u_{\pi,j\Delta}^2,$$

where  $\Theta_\pi \equiv (\sigma_\pi, \check{\pi}, \lambda_\pi, \sigma_a, \lambda_a)^\top$  and

$$u_{\pi,t+\Delta} = \pi_{t+\Delta} - \left[ \pi_t e^{-\lambda_\pi \Delta} + \hat{\pi}_t (1 - e^{-\lambda_\pi \Delta}) \right].$$

The updating rule for  $\hat{a}_t$  and  $\nu_{a,t}$  are provided in (B29) and (B30), respectively.